INSTITUT FÜR INFORMATIK der Ludwig-maximilians-universität münchen



Master's Thesis

Pixel-based 2-DoF Synthesis of 360° Viewpoints Using Flow-based Interpolation

Rosalie Kletzander

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Hiermit versichere ich, dass ich die vorliegende Masterarbeit selbständig verfasst und keine anderen als die angegebenen Quellen und Hilfsmittel verwendet habe.

München, den 26. Februar 2021

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Abstract

Virtual Reality technology allows users to experience virtual environments by interacting with them, and navigating within them. These environments tend to be either meticulously modeled in 3D by hand, or recorded using 360° cameras. The advantage of using 360° images is that a high level of realism is achievable with relatively little effort. However, the use of 360° images generally limits users to a single viewpoint or forces them to "jump" between different viewpoints. In order to improve the viewpoints based on captured viewpoints, in the best case enabling a user to navigate freely and naturally within a scene. There are a number of different approaches to image-based synthesis, many of which use some form of feature correspondence to extract the scene geometry from the captured images. While using the scene geometry makes it possible to synthesize novel views, it can also be problematic, since inaccurate scene geometry can lead to severe artefacts, and accurate scene geometry is difficult to obtain unless dedicated depth sensors are used.

In order to reduce the number and severity of these artefacts, this thesis proposes a pixelbased 2-DoF synthesis algorithm that combines basic reprojection with flow-based interpolation. Instead of estimating scene geometry, a sphere is used as a proxy for inaccurately estimated scene geometry. To mitigate the artefacts caused by the inaccurate geometry, flow-based interpolation is used to generate viewpoints with more accurate perspectives in a method called "flow-based blending". A proof-of-concept implementation of the approach is presented and tested with a select set of parameters, using different virtual and real scenes. The synthesized images are then evaluated based on mathematical error metrics, as well as on visible artefacts. The results of the evaluation show that in the majority of cases where the basic method produces significant artefacts, the synthesis using flow-based blending improves the accuracy of the results.

Zusammenfassung

"Virtual Reality" lässt Nutzer*innen durch Interaktion und Navigation virtuelle Welten erleben. Um diese Welten zu erschaffen, werden die Szenen meist zeitintensiv mit der Hand 3D-modelliert oder mithilfe 360° Kameras aufgezeichnet. Im Vergleich erreichen dabei die Aufzeichnungen mit 360° Kameras mit geringerem Aufwand einen hohen Grad an Realismus. Andererseits limitiert die Benutzung von 360° Bildern in der Regel die Bewegungsfreiheit der Nutzer*innen, da der Besichtigungspunkt entweder auf einen einzigen beschränkt ist oder von einem Besichtigungspunkt zum nächsten, "gesprungen" werden muss. Um das Besichtigungserlebnis zu verbessern und freie Navigation zu ermöglichen, gibt es den Forschungsbereich der Bildsynthese. Das Ziel dieses Forschungsbereiches ist es, neue Besichtigungspunkte anhand von existierenden zu berechnen. Dies kann im besten Fall dazu führen, dass Nutzer*innen sprungfrei und intuitiv innerhalb einer Szene navigieren können. Neben einer Vielzahl anderer Ansätze der Bildsynthese kann die Übereinstimmung in den Bildern verschiedener Besichtigungspunkten verwendet werden, um das geometrische Szenenmodell zu extrahieren. So können zwar neue Besichtigungspunkte berechnet werden. allerdings ist die Beschaffung eines präzisen Szenenmodells schwierig. Wird die Bildsynthese unter Verwendung von solchen fehlerhaften Szenenmodellen durchgeführt, können in der weiteren Berechnung schwerwiegende Artefakte auftreten, die das Nutzererlebnis erheblich beeinträchtigen.

Diese Arbeit präsentiert und evaluiert einen Ansatz, der die Anzahl und den Schweregrad dieser Artefakte zu reduzieren versucht. Der verwendete Algorithmus ist ein pixel-basierter Synthesealgorithmus mit zwei Freiheitsgraden, der grundlegende Reprojektion mit Interpolation basierend auf optischem Fluss kombiniert. Dabei wird Anstelle eines berechneten Szenenmodells eine Kugel als Proxy-Modell verwendet, welche ein fehlerhaft berechnetes Szenenmodell repräsentiert. Die Reduktion der durch die Abweichung vom tatsächlichen Szenenmodell entstehenden Artefakte erfolgt durch Interpolation basierend auf optischem Fluss. So werden Besichtigungspunkte mit einer passenden Perspektive generiert. Nach der Präsentation des Synthesealgorithmus mit sogenanntem "flow-based blending" wird dieser anhand einer Auswahl an Parametern in virtuellen und realen Szenen getestet. Die abschließende Untersuchung und Evaluation der berechneten Ergebnisse erfolgen mittels mathematischer Metriken und visueller Einschätzung. Dabei ist festzustellen, dass im Großteil der Fälle in denen der grundlegende Algorithmus ohne "flow-based blending" eindeutige Artefakte aufweist, die Synthese mit "flow-based blending" die Präzision der Resultate verbessert.

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1. Introduction

Over the past decade, Virtual Reality (VR) technology has experienced a resurgence in popularity due to the development of a number of affordable, consumer-quality head-mounted displays¹. These displays allow a user to experience and interact with a virtual environment in 3D, for example by playing games or by taking virtual tours of cities, historical landmarks, or remote locations in nature.

Some of these environments are modeled meticulously in 3D, while others use 360° images taken on location. Often, the 3D-modeled environments allow a lot of freedom of movement, enabling users to "walk" around and inspect elements of the scene at will. Unfortunately, modeling a real environment by hand to be viewed interactively requires an enormous amount of time and effort, and even then it is very difficult to achieve photo-realism. An alternative is to capture the location with a 360° camera, which records all of the surroundings in a single image. Viewing these images offers photo-realism (as they are actual photos), but often unnatural navigation, for example forcing the user to "jump" from one image location to the next, instead of being able to "walk" smoothly around the scene. Nevertheless, the ease of capturing 360° images with modern 360° cameras, along with the significant advantage of providing photo-realism, makes this an attractive method for creating immersive VR environments.

The difficulties of navigating an environment captured through 360° cameras are not a new phenomenon. Such problems are also relevant in virtual tours that exist outside of the realm of immersive VR, that are viewed on regular computer or smartphone screens, for example interactive tours of museums, real-estate, or other locations of interest. A prominent example is Google's Street View, which allows users to navigate streets and monuments around the world by way of 360° images.

Whether a scene is viewed stereoscopically with a head-mounted display or monoscopically on a flat screen, currently a significant obstacle is the problem of interactive, user-driven navigation. Ideally, users would be able to go anywhere they liked in the scene, and view anything they wanted from any angle and at any level of detail. Unfortunately, for environments captured by way of a 360° camera, this type of interaction would require a prohibitive amount of data, as well as being impossible to manually execute, since a separate image would have to be captured at every possible viewing position.

¹The price of a consumer-quality VR headset is between approximately 20 and 1000 USD as of January 2021, including headsets for use with a smartphone.

⁽https://www.tomsguide.com/us/best-vr-headsets,review-3550.html, accessed Jan 13, 2021)

1. Introduction

An alternative to capturing all of these viewpoints manually is to generate them digitally. This requires capturing a much smaller subset of images and using these to synthesize the desired, novel viewpoints. Generating new images based on already captured images is generally known as *image-based rendering* (IBR), or *image-based synthesis*. There are many different approaches to synthesizing new images from captured ones, and they can generally be categorized in two different ways:

- by the spacial limitations imposed by the synthesis technique, including degrees of freedom and range of motion
- by the type and amount of information extracted from the captured images

The area and the degrees of freedom (DoF) required for navigation usually depend on the goal and requirements of the application: A virtual tour on a pre-defined path, for example, would only require generating intermediate views between existing viewpoints (i.e. synthesis with 1-DoF) for a smooth transition. For a less constrained virtual tour that enables users to navigate freely on a plane, generating viewpoints with 2-DoF at eye-level could be sufficient. Users could move around and look in any direction but not change their viewing height. Some applications may require 3-DoF, for example in order to enable users to closely inspect certain objects from all angles, but restrict them from moving away from the object.

Depending on the type of scene, the required fidelity, and the real-time requirements, different IBR techniques leverage different amounts and types of information extracted from the input images. For example, there are approaches that extract as much geometry information as possible from the set of images and try to reconstruct the 3D geometry of the scene as closely as possible. These approaches can suffer from the problem of extracting accurate geometry information, since errors in geometry can lead to unappealing results. Other approaches try to extract some information from the image, such as feature correspondences, or motion vectors (optical flow), which enables interpolation between pairs of images, i.e. a smooth transition with 1-DoF. Finally, there are approaches that use no semantic image information whatsoever. Instead, they may use color values, simple proxies for the scene geometry, or information about the relative location of captures, but they tend to operate on a pixel level. Although there is no specific label for this kind of synthesis, for the purpose of this thesis, it will be referred to as *pixel-based synthesis*.

One very basic form of pixel-based synthesis is to use a simple proxy ("stand-in") geometry, for example a sphere, in place of the real scene geometry². This allows for resampling the captured images in order to create a new viewpoint at any location within the scene without having to estimate or record the actual scene geometry. However, a significant difference between the proxy and the actual geometry can lead to severe distortions and artefacts in the resampled images. Although this basic form of pixel-based rendering using proxy geometry may be unsuitable for scenes where the real geometry differs greatly from the proxy geometry, it may be possible to improve these results by combining the basic technique with a 1-DoF interpolation method.

²The term "proxy geometry" is used in this thesis as a term for the model used in place of the real scene geometry. It can be anything from a simple geometric shape such as a sphere, to a simplified version of the real scene geometry.

Problem Statement

A number of 1-DoF interpolation techniques exist, many of which use some form of feature correspondence. Flow-based interpolation is one of these techniques that has already been used successfully for 360° images. It uses motion vectors ("optical flow") between pairs of images to interpolate new viewpoints between them. The goal of this thesis is to answer the following research questions:

- 1. Can flow-based interpolation be used in pixel-based 2-DoF synthesis with proxy geometry?
- 2. How does the flow-based interpolation affect the accuracy of the synthesized images compared to the basic pixel-based synthesis?

In order to measure the accuracy of the different results, the synthesized images are compared with the ground truth images using two different error metrics, as well as being assessed visually.

Methodology

The methodical approach used in this thesis consists of two distinct phases which address the two research questions: The first phase (the "implementation phase") aims to design and implement a pixel-based 2-DoF synthesis with proxy geometry using flow-based interpolation. The second phase (the "evaluation phase") aims to examine whether the flow-based interpolation can improve the results of the basic synthesis without flow-based interpolation. Figure 1.1 shows the details of the methodical approach, including these two phases, along with the inputs and the results of the process.

For the implementation phase, a pixel-based synthesis algorithm using proxy geometry is developed, labeled "synthesis with regular blending". Then, the synthesis with regular blending is adapted to incorporate an existing flow-based interpolation algorithm (the input to the implementation phase in Figure 1.1). The resulting flow-based synthesis algorithm is labeled "synthesis with flow-based blending". The development of this proof-of-concept algorithm proves that it is possible to leverage flow-based interpolation for pixel-based 2-DoF synthesis with proxy geometry, which is the first result, shown at the bottom of Figure 1.1.

The algorithms developed in the implementation phase are then tested and evaluated in the evaluation phase. The evaluation phase is further divided into three steps, separated vertically in Figure 1.1: preparation, synthesis and testing, and evaluation. In the preparation step, data for testing and evaluation is acquired based on the defined parameter space, including virtual and real scenes. Then, the images are synthesized with both the regular blending and the flow-based blending algorithm, which are the output of the implementation phase. The resulting images are then compared with the ground truth data using the error metrics adapted for 360° images. Finally, using the calculated error values, along with the synthesized images, the results are analyzed and evaluated. This full evaluation is the second result of the thesis.



Figure 1.1.: Methodical approach

Scope

As the number of possible different environments is infinite, as well as the positions at which images can be captured, it is necessary to limit the parameter space for testing and evaluation. First of all, only indoor scenes are examined. The scenes are assumed to be static, meaning the objects within the scene do not change their positions. To reduce the complexity of the implementation, as well as the number of necessary input images to be captured, only 2-DoF synthesis is considered. Specifically, all captured and synthesized viewpoints are located on a plane at approximate eye-level parallel to the ground. The parameters that will be examined in detail are:

- **Difference between the scene geometry and the proxy geometry** The proxy geometry used in this thesis is a sphere of the approximate size of the scene. Scenes of different basic shapes, containing different objects, are tested in order to gauge the effect of the difference between the proxy geometry and the scene.
- **Density of captured viewpoints** The density of the captured viewpoints is an important aspect of the process of IBR, as it is directly related to the effort required to capture a scene. The higher the necessary density for successful synthesis, the more images need to be captured, which requires more manual effort. In order to assess the effect of different densities on the accuracy of the results, different densities of captured viewpoints are tested.
- **Position of synthesized points relative to captured points** A synthesized viewpoint can theoretically be located anywhere within the boundaries of the scene, as long as it is at the defined eye-level. The relative position of the synthesized point to the captured points is likely to have an effect on the accuracy of the result and will be examined in more detail by synthesizing a dense grid of viewpoints within a scene.

These parameters will not be examined exhaustively, as this is impossible, given the infinite possibilities of scene shapes and object placements. Instead, for each parameter to be examined, a scenario is designed that tests this parameter in a feasible context.

Contributions

The contributions of this thesis are:

- An algorithm for pixel-based 2-DoF synthesis with flow-based interpolation ("synthesis with flow-based blending")
- A basic proof-of-concept implementation of this algorithm
- An evaluation of the results of this algorithm, including a comparison with the results of the algorithm with regular blending

The results show that in the majority of cases where the basic method with regular blending produces significant artefacts, the synthesis using flow-based blending does improve the accuracy of the results.

1. Introduction

Outline

In order to understand the underlying concepts and techniques that are used in the synthesis approach proposed in this thesis, Section 2.1 introduces the fundamentals of 360° images and optical flow, followed by related work in the field of image-based synthesis in Section 2.2. Based on this information, Section 3 presents the approach and implementation details of the pixel-based 2-DoF synthesis algorithm with regular blending and flow-based blending. Then, in order to understand how the algorithm is evaluated, the evaluation parameters and methodology are presented in Section 4.1 and Section 4.2, followed by the evaluation of the virtual scenes based on the selected parameters in Section 4.3 and the proof-of-concept evaluation of the real scene in Section 4.4. Based on the results of these evaluations, the limitations of the evaluation are discussed in Section 4.5. Finally, building on the insights gained in the evaluation, avenues for future work are presented in Section 5, along with the conclusion of the thesis.

2. Background and Related Work

This chapter outlines the basic concepts and methods used in the approach (Section 2.1), and presents the state-of-the-art of image-based rendering techniques (Section 2.2).

2.1. Fundamentals

The images used in this thesis, as well as many other approaches, are 360° images. Since 360° images differ significantly from "regular" images in how they are captured and visualized, it is important to understand how 360° cameras capture their surroundings, how the captured data can be mapped to a planar surface, and what the most common mappings for 360° images are (Section 2.1.1). Also, the concept of optical flow is introduced, as it is a prerequisite for a number of image-based rendering techniques, including the flow-based interpolation used in this thesis (Section 2.1.2).

2.1.1. 360° Images

Capturing an image with a 360° camera differs significantly from capturing an image with a regular camera. A regular camera captures incoming rays of light with a limited field of view, as shown in Figure 2.1a: Only the light rays from the tree on the right are captured, since this is the direction the camera is facing. The sensors on the camera (or the film, for analog cameras), are arranged on a plane and register the wavelengths of incoming rays from this direction. This process represents a projection of the scene onto a plane. The measured light values can then be stored directly as a planar image.

A 360° camera¹, on the other hand, captures light rays with an field of view of 360° . This means that the sensors are arranged such that they capture light rays from the entire surroundings, as shown in Figure 2.1: Instead of capturing only the tree on the right, the 360° camera captures all of the surroundings. For the sake of simplicity, the sensors of a 360° camera can be pictured as a number of sensors in the form of a sphere². This means that the initial capture of light rays represents a projection of the scene to a sphere. The camera must then perform an additional conversion in order to transform the light values captured on a sphere to a planar image, depicted in Figure 2.1b. [SI14]

The projection onto a flat surface is necessary, since image data is generally stored in 2D, and the majority of viewing devices are planar (e.g., computer or smartphone screens). The process of translating data from a 3D model to a 2D image and vice versa is well known in computer graphics and is called *uv mapping* or *texture mapping*.

¹The term "omnidirectional camera" is also used informally, however, this term is less exact, since an omnidirectional camera can also be a camera that captures a single hemisphere, instead of the full scene [SI14].

²The sensors cannot actually take the form of a perfect sphere, since the camera needs to have some form of casing. Instead, several lenses are usually used ("polydioptric cameras" [SI14]), and the image stitched together in software.

2. Background and Related Work

Specifically, the process of uv mapping for spherical geometry is needed to map the data from the sphere to a planar image. This process describes a reversible operation in which the points (x,y,z) on the sphere (described by *unit directions* which are unit vectors) are associated with pixel positions in image coordinates (u,v). Figure 2.2 shows an example mapping between the unit sphere and a planar image. In this example, the poles of the sphere are mapped to the entire top and bottom pixel rows of the image, and the equator is mapped to the row of pixels in the vertical center of the image. This means that the areas near the poles are *oversampled*, which indicates that the mapping function is not *equal area* [RWPD05, p.450] i.e. it does not conserve how much area a pixel value occupies.

In the case of a 360° camera that is mapping the captured light rays to a planar image for storage, the image values are some type of color values. However, other kinds of information can also be uv-mapped to a shape, for example illumination data, depth values ("bump mapping"), and more.

The most common mappings for 360° images are the *cube map*, the *ideal mirrored sphere*, the *angular map*, and the *equirectangular map* [RWPD05, p. 535]. The image data can be projected using any of these mappings with only minimal data loss from interpolation. These mappings are depicted in Figure 2.3: The left column shows the different mappings of a 360° image, and the right column displays a representation of the approximate image directions in order to visualize the distortions introduced by the different mappings. These four most common mappings are briefly presented in the following paragraphs.

Cube Map The cube map is a mapping that splits the image data into six separate square views, one in each direction (top, front, left, right, back, bottom). This is the equivalent of capturing the surroundings with six different cameras with a field of view of 90° each, and then stitching the resulting images into a shape that can be "folded" into a cube (see Figure 2.3a), which also gives this mapping its name.

Due to the projection of a spherical surface to a plane, there is some distortion towards the edges of each face. However, this distortion is comparable to the distortion at the edges of a regular, planar image, which is a significant advantage compared to other mappings (see Figure2.3b,d,f,h³). A disadvantage is that each face is projected separately, which leads to directional discontinuities at the many seams. This type of mapping is often used to simulate complex environments in 3D scenes (e.g., for game or animation graphics), as it is easy to use and reduces render time significantly compared to a 3D model of the same environment. [RWPD05, p. 540]

Ideal Mirrored Sphere The ideal mirrored sphere is a mapping to a circle within a square (see Figure 2.3c). It represents how the surroundings would be reflected if one placed a small sphere with a perfectly reflective surface ("mirrored" sphere) into a scene and then photographed it using an orthographic camera. This mapping, like all the mappings presented here, shows the complete surroundings, albeit considerably distorted toward the edges. Figure 2.3d shows where each direction is mapped and the extent of the distortion. It is clear that the farther away from the "front" area, the more distorted the mirrored sphere mapping is. The ideal mirrored sphere mapping can be used for calculating average illumination color

³Figure 2.3b does not perfectly represent the distortion in cube maps. It was chosen as a baseline because cube maps have relatively little distortion compared to other mappings and it visualizes which parts of the image are mapped where and how they are distorted in other mappings.



(a) Image capturing process with a regular camera: The sensors are arranged on a plane, so capturing the rays corresponds to a projection to a plane.



(b) Image capturing process with a 360° camera: The sensors are arranged in an approximation of a sphere, which means an additional step is needed to convert the captured data to a planar representation.

Figure 2.1.: Capturing an image with a regular camera compared to a 360° camera



Figure 2.2.: Example of uv mapping for spherical geometry

for high dynamic range calculations; however, the type of distortion at the edges can cause problems with sampling, which is why the angular map mapping, presented next, tends to be preferred. [RWPD05, p. 535]

Angular Map At first sight, the angular map seems very similar to the ideal mirrored sphere. It also maps to a circle within a square, however it samples the input in such a way that the back of the image is allotted more space and is less distorted than the mirrored sphere (see Figure 2.3e and Figure 2.3f). [RWPD05, p. 537]

Equirectangular Map The equirectangular, or latitude-longitude ("latlong") mapping is a common type of mapping in cartography. The data is mapped to a rectangular image space, in which the width is twice the height. The azimuth (around the circumference) of the sphere represented by the unit directions/vectors is mapped to the map's horizontal coordinate and the elevation to the vertical coordinate (see Figure 2.3g). The main problem of this representation is well known in cartography: The distortion increases significantly towards the poles, as can be seen in Figure 2.3h. Otherwise, this mapping is convenient as it has very few seams and all pixels are valid (i.e. there are no "black" areas). It is used as a storage format for 360° images. [RWPD05, p. 538]

While all of these projections are static, showing the entirety of the 360° image at once, it is also possible to view 360° images interactively. In this case the field of view tends to be limited, so only a certain part of the image needs to be projected: the part of the image the viewer is "facing" virtually. Once the viewing direction has been determined, the projection can be calculated such that the center of the image has minimal distortion. Any of the above projections can be used for this.

2.1.2. Optical Flow

Optical flow describes the displacement of specific points between two images. It is generally used on consecutive frames of video sequences, for example for semantic segmentation, structure-from-motion, data compression or other applications where information about movement between images is required. To illustrate, Figure 2.4 shows two consecutive frames of a video sequence. On a high level, an optical flow algorithm should recognize that the pixels representing the bicyclist are moving towards the bottom left of the image, and the pixels representing the background are moving to the right (because the camera is panning slightly to the left).

There are two types of optical flow: sparse optical flow and dense optical flow. Sparse optical flow algorithms calculate the motion of several select points that can be either chosen manually, or by some kind of automatic selection (e.g., based on features). This type of optical flow can be used to track only specific objects in a scene (e.g., the direction and relative velocity of a certain car in traffic).

Dense optical flow algorithms compute the motion of *each pixel* between two images, instead of single points. This can be used for more general object tracking (e.g., direction and relative velocity of complete surroundings in traffic), to estimate 3D geometry (in structure-from-motion algorithms), or to identify static sections of the image for video compression [FBK15]. Dense optical flow can also be used for image synthesis, such as in Richardt et al.'s

2.1. Fundamentals



(a) Cube map example



(c) Mirrored sphere mapping example



(e) Angular mapping example



(g) Equirectangular (latlong) mapping example



(b) Cube map distortion visualization



(d) Mirrored sphere distortion visualization



(f) Angular mapping distortion visualization



(h) Equirect angular distortion visualization

Figure 2.3.: Common mappings for 360° images

Megastereo [RPZSH13] described in Section 2.2.2, which is also the basis of the flow-based interpolation presented in this thesis.

There are a number of optical flow algorithms, ranging from methods using parametrization, or regularization [FBK15] to methods relying on Deep Learning [SET20]. Although these algorithms differ greatly in approach, they share the type of result, which is a vector field. For dense optical flow, this vector field contains a vector for each pixel, describing the displacement of this pixel between the input images. Sparse optical flow only contains a vector for each pre-chosen point, not for every pixel.

Figure 2.5 shows two different visualizations of the vector field calculated by the dense optical flow algorithm by Farnebäck [Far03] between the frames in Figure 2.4. Figure 2.5a is a color-based visualization: the hue encodes the vector direction and the saturation encodes the vector length for each pixel. Using this visualization, it is possible to roughly distinguish two separately moving areas of the image, which could be used for semantic segmentation. Figure 2.5b shows the pixel displacements with vectors: The vector orientations and lengths are represented by arrows.

These visualizations can help show if and how well an optical flow algorithm is working. Although there are a large number of different algorithms, most of them still do not effectively deal with common issues such as occlusions, too-large displacements and intensity changes [FBK15]. Occlusions are problematic, since the displacements between two images may reveal or cover image areas that, as a result, have no correspondence in the previous image. This problem is exacerbated when displacements are very large (e.g., due to fast-moving objects). Large displacements are also problematic by their very nature, as most algorithms are not designed to handle them. How these limitations affect the use of optical flow for image synthesis will be discussed in Chapters 3 and 4.

2.2. Related Work

Image-based rendering (IBR) and viewpoint interpolation⁴ started attracting interest with the advent of virtual walkthroughs, for example for Apple's QuickTime[®] VR, in order to save render time by generating views from images instead of using complex 3D scenes including textures, lights and complex geometric models [Che95]. Chen and Zhang, in their survey on image-based rendering [ZC04], use the terms *source description* and *appearance description* to compare these basic rendering techniques: "Traditional" rendering techniques use *source description*, i.e. the scene is described by the objects within it, their positions and properties. On the other hand, IBR techniques try to achieve the same goal through *appearance description*: Instead of trying to describe the scene through the objects it contains, image-based rendering techniques try to model the *light rays* that reach the viewer. The reason why this is feasible is that human vision itself has little to do with 3D geometry; it is the processing of a dense set of light rays by the brain which are "captured" by the eye. This process can also be performed by a capture device like a camera. As a result, it is not necessary to meticulously model the source, it is sufficient to model the "appearance" (i.e., the light rays) of a scene.

⁴As there seems to be no explicit difference between the terms "image-based rendering", "viewpoint interpolation" and "viewpoint synthesis" in the literature, they will be used interchangeably in this thesis, although "interpolation" is favored for simpler blending techniques, and "synthesis" is used to describe more complex algorithms.



(a) Frame 1

(b) Frame 2





(a) Visualization of optical flow with color: the hue encodes the vector direction, the saturation encodes the vector length for each pixel.



(b) Visualization of optical flow with arrows: The vectors are represented by arrows (only a limited number of vectors are shown)



2. Background and Related Work

While the differentiation between source description and appearance description is helpful for understanding the basic differences between image-based and traditional rendering, many image-based rendering methods also utilize some form of source description, predominantly in the form of 3D geometry. In a different survey on image-based rendering techniques, Kang and Shum [SK00] classify IBR rendering techniques on a continuum, which ranges from techniques using no geometry, to techniques using implicit geometry (or more generally, feature correspondences), to techniques using explicit geometry.

The algorithm presented in this thesis is a combination of two different approaches: the first step uses no geometry whatsoever, and the second step uses feature correspondences to correct some of the problems that arise in the first step. This differentiation guides the related work presented here: The first section presents synthesis approaches using no geometry, and the second section presents approaches using implicit geometry or feature correspondences.

2.2.1. Image Synthesis without Image Correspondences

A theoretical model for image synthesis with no geometry or other image features (i.e., "pure" appearance description) was developed by Adelson et al. [AB91]: the *plenoptic function* shown in Equation (2.1). The plenoptic function is a 7D function that describes the observable light at every point in space V_x , V_y , V_z , from every direction θ , φ , at every wavelength λ , at every possible point in time *t*.

$$P = P(\theta, \varphi, \lambda, t, V_x, V_y, V_z)$$
(2.1)

In practice, it is infeasible, if not impossible, to cover all dimensions of this function, as this would require a capture device at every location, at every point in time, capturing light rays coming from every direction. However, by making different assumptions, IBR techniques try to reconstruct simplified versions of the plenoptic function. Common assumptions are the reduction of wavelengths to RGB, the removal of the temporal dimension, and the assumption that the light is constant along a ray in empty space (i.e., light does not change its wavelength over distance) [ZC04]. The methods for resampling the plenoptic function, or a lower-dimensional version are diverse, from Light Field Rendering [LH96], which uses a capturing rig to uniformly sample the surroundings with a very high sample rate, and is able to construct views in real time, to more recent approaches that use neural networks to enhance the captured samples [NJ18], or even predict light fields, or "radiance fields", themselves [MST⁺20]. The following section presents approaches that concern themselves specifically with 360° images, as this is most relevant for this thesis.

"A Simple Method for Light Field Resampling" [Kaw17]

Kawai [Kaw17] approaches the problem of synthesizing new images with two degrees of freedom without using 3D geometry. Their basic setup is to capture four 360° images at each corner of a rectangular area and use resampling to synthesize a new image anywhere within this area.

The resampling is done by inserting a virtual sphere centered at the synthesized viewpoint representing a projection screen on which to project rays from the captured viewpoints. The locations of the captured viewpoints are known, so the outbound rays of these viewpoints can be calculated by using the image-to-world coordinate conversion from the equirectangular representation. The intersections of these captured rays with the virtual sphere are calculated and the corresponding pixel values are used. The areas of the projection screen where no rays have intersected are approximated by repeating the reprojection at different resolutions.

In cases where several rays share an intersection, Kawai proposes several methods. The first is to take an average of the rays. As an alternative, they suggest employing a rating based on the inner product of the ray direction and the viewing direction and using the ray with the smallest score. A final option is to prioritize one specific captured viewpoint over the others to completely avoid ghosting artefacts.

To evaluate their method they capture four viewpoints in a scene (the distances between the viewpoints are not mentioned) and calculate an image along a diagonal. They then compare the results of the different ray combination methods by describing visual artefacts.

"On the Use of Ray-tracing for Viewpoint Interpolation in Panoramic Imagery" [SLDL09]

Shi et al. [SLDL09] examine how ray tracing can be used to calculate arbitrary new viewpoints based on knowledge of relative positions between the viewpoints which are stored as cube maps. For every pixel in the target image, a ray is cast into the scene. Since the geometry of the scene is unknown, an alternative method is used to find the correct value of that point. They do this by introducing a color consistency constraint, which compares the pixel values of the rays cast from all the reference images. The assumption is that if the colors of different rays are the same, the rays must be intersecting the same point.

In order to calculate an intersection with the scene, they propose two different methods: a brute-force depth search using no scene geometry which searches along all of the captured rays until the pixel values are similar enough to fulfill their color constraint requirements, or a guided depth search using sparse 3D reconstruction.

To evaluate their method, they use a set of five captured input images with a maximum distance of 1m, from which they remove one to use as ground truth. They evaluate the algorithm by comparing the brute-force to the guided depth search based on the artefacts in the results and the computation time.

"Unconstrained Segue Navigation for an Immersive Virtual Reality Experience" [HDR⁺17]

Herath et al. [HDR⁺17] propose a system that enables casual users to capture their surroundings in a grid with a smartphone, and then navigate that environment with two degrees of freedom. In order to interpolate between two captured 360° images (1-DoF), they differentiate between faces that are parallel to the axis of movement and faces that are perpendicular to the axis of movement. For faces that are parallel, they stitch the faces of two adjacent viewpoints together and interpolate by using a sliding window. For faces that are perpendicular, they calculate a homography between the faces of two adjacent viewpoints and morph the image accordingly. To interpolate any image within a rectangular area bounded by four captured viewpoints (2-DoF), they recursively interpolate intermediary viewpoints until they reach the desired position.

As the focus of their work is on the whole process of capture, navigation, and viewing, the interpolation step is not explicitly evaluated.

2.2.2. Image Synthesis using Image Correspondences

Leveraging image correspondences for synthesis has been a popular method almost since the beginning of viewpoint synthesis. Chen and Williams [CW93] were one of the first to use "the morphing method" that simultaneously blends the shape and texture of two images using image correspondences. A comparable method, based on optical flow, is used by Richardt et al. [RPZSH13] for planar images.

Adapting planar algorithms (e.g., optical flow, structure-from-motion) for 360° images is a common challenge in 360° image synthesis. Kolhatkar et al. [KL10] and Huang et al. [HCCJ17] solve this problem by extending the faces of the cube maps to account for pixels moving across borders. [KL10] then use optical flow for interpolation between two images; whereas [HCCJ17] estimates the scene geometry with a structure-from-motion algorithm to extend monoscopic 360° videos to stereo. Zhao et al. [ZWF⁺13] propose a method for adapting sparse correspondence matching for the spherical domain, circumventing the need to use an extended cube map.

Morphing the images to create a new viewpoint can be done with pixel-based blending [RPZSH13], [KL10] or by triangulating the image and calculating homographies between the triangles [HCCJ17], [ZWF⁺13].

The flow-based blending approach in this thesis builds on the approaches of [RPZSH13] and [KL10], which are presented in more detail in the following sections.

"Megastereo: Constructing High-Resolution Stereo Panoramas" [RPZSH13]

Richardt et al. [RPZSH13] present an approach which combines planar images captured casually on a radius to create a panoramic image that is viewable in stereo in high resolution. In place of scene geometry, they use a cylindrical imaging surface that is concentric to the capture center. For each eye at a given viewing orientation, they project a ray into the scene, represented schematically in Figure 2.6a. Then, they calculate the deviation angle α between the desired ray and the nearest captured rays. Figure 2.6b illustrates this process: \widetilde{I}_{M} (the blue camera) is the desired viewpoint and I_{K} (green camera) and I_{L} (red camera) are the captured viewpoints. The point F is the intersection point with the cylindrical imaging surface, which determines which rays are to be used. The deviation angle α_1 and α_2 are the angles between the determined rays from the captured viewpoints I_{L} and I_{K} , respectively.

Linearly blending the rays (i.e., adding the weighted pixel values) of the two closest captures would lead to artefacts due to the difference between the real geometry and the cylindrical surface. This is shown in Figure 2.6c: Since the captured object (the tree) is behind the cylindrical imaging surface, some points (e.g., C, captured at c^{I} and d^{I}) are captured by different rays at different places on the imaging surface. This results in doubling effects in the resulting image (shown in the top left corner of Figure 2.6c). To mitigate this problem, Richard et al. propose a "flow-based blending" technique: For each ray of the final image that is not a captured ray (deviation angle 0), a new ray is synthesized using optical flow. Figure 2.6d shows how the point P, "captured" by the synthesized ray and projected to position \tilde{p} on the cylindrical imaging surface is interpolated: The two closest viewpoints I_{K} and I_{L} are used to interpolate \widetilde{I}_{M} using the optical flow vector F. The pixel at position \tilde{p} is then taken from this new viewpoint which corresponds to the matching ray.

The interpolated image I_M at point η between the images I_K and I_L is calculated by shifting I_K by $\eta \cdot F_{k \to l}$ and by shifting I_L by $(1 - \eta) \cdot F_{l \to k}$. The two shifted images are then blended



Figure 2.6.: (a) Illustration of rays required for creating a stereoscopic panorama and (b) deviation angles α. (c) Duplication and truncation artefacts caused by the aliasing. (d) Flow-based upsampling to synthesize required rays. Adapted from [RPZSH13]

linearly, using η as the weight. Instead of calculating the entire image for each ray, only the necessary image areas are extracted and the interpolation is calculated pixel-wise.

To evaluate their method, they leverage datasets used by other approaches, as well as capturing their own images. They visually compare the results, noting improvements based on visible artefacts.

"Real-Time Virtual Viewpoint Generation on the GPU for Scene Navigation" [KL10]

Kolhatkar and Laganière [KL10] propose a method for smoothly interpolating between pairs of 360° images. Their approach is similar to the approach in Megastereo, where optical flow between the images is used to incrementally morph the two images. In order to adapt the optical flow calculation for 360° images, they extend the cube map representation to account for points moving across edges, which is the method that is used in this thesis, as well. To reduce artefacts in the obtained optical flow, they perform a matching and smoothing step. They then implement their algorithm on the GPU, which allows them to interpolate between images in real-time.

They evaluate their method by capturing scenes at "reasonable" distances and removing every other image in order to obtain ground truth data. The computation time of the optical flow calculation of the extended cubes is measured, as well as the actual interpolation time. Furthermore, they compare the interpolated results with ground truth images, both visually and by using a per-pixel metric.

2.2.3. Discussion

The overview of the presented approaches in Table 2.1 shows that most of the approaches using sparse features or optical flow, in the third column of Table 2.1, only allow for synthesis with 1-DoF. On the other hand the approaches using no correspondences (the first three in the third column) allow for synthesis with 2-DoF. [HCCJ17], which uses dense geometry is an exception to this rule, since it offers 3-DoF; however, in this case, the movement range is

	method			evaluation					
	input type	DoF	extracted features	defined parameter space?	visual eval.	error metrics	compu- tational cost	comparison to other approaches	
[Kaw17]	360° images	2	none	×	1	×	1	×	
[SLDL09]	360° images	2	none/ dense geo	(🗙)	1	×	1	×	
[HDR ⁺ 17]	360° images	2	none	×	×	×	1	×	
[RPZSH13]	planar images	1	dense flow	×	1	×	1	1	
[KL10]	360° images	1	dense flow	×	1	1	1	×	
[HCCJ17]	360° video	3*	dense geo	×	1	×	1	1	
[ZWF ⁺ 13]	360° video	1	sparse feature	(🗙)	1	1	1	1	

*on a constrained path

Table 2.1.: Comparing the methods and evaluations of different approaches

constrained and users need to stay close to a pre-defined path. There is no approach that attempts image synthesis with 2-DoF using optical flow.

As for the evaluation, none of the approaches test their methods on a defined parameter space. The only approaches that declare which parameters were used for the presented examples are [SLDL09] and [ZWF⁺13] (marked in parentheses in the fourth column in Table 2.1). Almost all approaches examine their results visually, remarking on artefacts, but only two use dedicated mathematical error metrics. All of the approaches evaluate the computational cost, whether they have a real-time requirement or not. Finally, only [RPZSH13], [HCCJ17] and [ZWF⁺13] compare their methods to other approaches. In general, the tests presented in the approaches are mostly based on a very small sample set. In addition, the evaluations are not methodical, and in some cases the parameters that are used (e.g., distance between captures) are not even described.

3. Pixel-based 2-DoF Synthesis of 360° Viewpoints with Flow-based Blending

The approach introduced in this chapter combines two types of methods presented in the previous chapter: At its base, the pixel-based synthesis with proxy geometry uses no scene geometry or correspondences whatsoever. It is similar to Kawai's "A Simple Method for Light Field Resampling" [Kaw17] in that it also uses a sphere to resample the surroundings. However, where Kawai's work suggests using only one viewpoint for resampling to avoid ghosting artefacts (i.e., doubled edges), the pixel-based synthesis presented in this chapter uses flow-based blending to try to remove ghosting artefacts. The flow-based blending is based on the method presented in Richardt et. al's Megastereo [RPZSH13].

First, the general approach to the synthesis with regular blending and flow-based blending is presented (Section 3.1) and then the details of the implementation are described (Section 3.2).

3.1. Approach

This section presents the assumptions and simplifications made for the pixel-based synthesis of 360° viewpoints (Section 3.1.1), the basic pixel-based approach using "regular blending" (Section 3.1.2) and an improvement to the basic approach based on flow-based blending from Richardt et al.'s Megastereo [RPZSH13] (Section 3.1.3).

3.1.1. Assumptions

In order to simplify the process of synthesis, some assumptions are made based on the scene and the viewpoints in the scene:

- the scene is static
- all images are captured on a plane parallel to the floor (viewpoint plane)
- all synthesized viewpoints are located inside the scene boundaries and are also located on the viewpoint plane
- the positions and orientations of the captures are known
- the scale (approximate radius) of the scene is known

Furthermore, for the moment, it is assumed that the optical flow algorithm used in the flow-based blending calculates an acceptable result between any pair of viewpoints.

3.1.2. Basic 2-DoF Synthesis using Regular Blending

With these assumptions and using a proxy geometry with approximately the same scale as the captured scene, it is possible to synthesize new viewpoints with varying accuracy, depending on the scene. The process presented here for basic 2-DoF synthesis with regular blending is a combination of texture lookup through raytracing, and mosaicking by using a constraint based on the ray deviation angle, which is referred to as "regular blending".

Raytracing-based Texture Lookup

The first step is to map the texture (i.e., pixel values) of an existing viewpoint to a new viewpoint according to its position in the scene. Theoretically, any 360° viewpoint can be mapped to any other, since each 360° image captures every point in the scene. This is only theoretically the case, since image resolution and occlusions in the scene will conceal some areas from some viewpoints whereas they are visible for others. However, at this point, this will be ignored and it will be assumed that each image contains all the points of the scene albeit at different image coordinates and different sampling rates¹.

In addition, 3D geometry of the scene is needed for raytracing. However, since the approach in this thesis does not capture or infer any real geometry, a proxy geometry is used that has approximately the same scale as the scene that was captured. The proxy geometry is a sphere, as this is a simple, very general geometry to represent a variety of different scenes. The radius of the sphere is chosen so that the sphere contains all possible points in the scene, for which the scale of the scene needs to be known. Under these assumptions, it is possible to map the image at one viewpoint to a new position by combining raytracing and texture lookup.

In order to do this, several steps of raytracing are necessary, which are visualized in Figure 3.1. Figure 3.1a shows how a camera at a specific viewpoint captures the light rays reflected from the objects in the scene. The captured pixel values are visualized on a circle around the center of projection of the camera (for simplicity's sake, only one row of pixels is shown). Once the viewpoints have been captured (there is only one viewpoint in this example), a new viewpoint is ready to be synthesized. The proxy geometry is visualized as a circle² in Figure 3.1b, with the new viewpoint to be synthesized represented by a dotted circle around a center of projection. For each pixel of the synthesized image, a ray is projected into the scene (Figure 3.1c) and its intersection with the scene is calculated. Then, the ray from the center of projection of the captured viewpoint to the scene intersection is calculated, which, when normalized, is equivalent to a unit direction vector of the unit sphere. Using the unit direction and the image mapping function, the pixel value at that position is retrieved (Figure 3.1e) and copied back to the new viewpoint (Figure 3.1f). In this way, the pixel values (i.e., texture) of a captured viewpoint are mapped to the new viewpoint (Figure 3.1g). Figure 3.1h compares the mapped values to the actual scene. It is immediately clear that most points have the value they would have had, had the viewpoint been captured instead of synthesized (ground truth value); however some are incorrect. This is due to the disparity between the proxy geometry and the real scene geometry.

¹By design, areas closer to the camera are captured with a higher sampling rate per point than areas farther away.

²In this example, the sphere does not surround the complete scene (the corners of the scene are outside the circle). This is only for visualization purposes, normally the sphere would contain the complete scene, including the corners.



(a) The real scene viewed from above: The camera captures light rays reflecting from objects.



(c) A ray for each pixel in the synthesized viewpoint is traced to its intersection with the proxy geometry.



(d) For each ray, a texture lookup is performed.



(b) A new viewpoint to be synthesized using the proxy geometry (sphere).



(e) From the intersection of the ray and the proxy geometry, a second ray is traced to the center of projection of the captured viewpoint and the pixel value is looked up.



(f) The pixel value is copied back to the new viewpoint.



(g) This process is repeated for all pixels.



(h) The resulting texture mapping from the captured viewpoint to the proxy geometry in comparison with the original scene.

Figure 3.1.: Process of texture lookup through raytracing



Figure 3.2.: Choosing the appropriate viewpoint to improve the result

Deviation-angle-based Mosaicking

The example in Figure 3.1 contains only one captured viewpoint, so the choice of which viewpoint to use for texture lookup is trivial. In cases where several viewpoints are available, a choice must be made as to which viewpoint should be used. In the case where the real scene has the same geometry as the proxy sphere, this choice is inconsequential, since the raytracing is always accurate. However, this scenario is unrealistic, since the number of spherical rooms containing no objects is negligible. Thus, as soon as the real scene differs from the proxy sphere, some viewpoints yield better results than others. Figure 3.2a shows how a discrepancy between the real scene and the proxy sphere can lead to inaccurate results: Since the intersection point of the rays with the scene is not accurate, the reprojection of viewpoint vp1 to the synthesized viewpoint S results in a white pixel for the depicted ray, although the ground truth value is purple.

When comparing rays from different viewpoints, two metrics can be examined: the euclidean distance of the captured viewpoint from the synthesized viewpoint and the deviation angle between the rays. Figure 3.2b visualizes the two metrics and in the example, the viewpoint vp2 with the smaller deviation angle is a better match. In fact, assuming that there is no obscuring element in the air such as fog, and disregarding diffusion and scattering over distance, the same light ray is captured by any viewpoint located on the ray in question. This means the closer the deviation angle is to zero, the more accurate the result will be, regardless of the distance of the viewpoints. In this simplified scenario, the best viewpoint would have a deviation angle of zero (Figure 3.2c). However, sampling rates and resolution also have an effect on the sampled point, so the euclidean distance cannot be completely ignored.

Instead of combining these metrics in a function that might have to be weighted differently depending on the scene size, the distribution of the viewpoints, or other factors, the choice of which viewpoints to use is divided into two different steps: the pre-selection of input viewpoints from all captured viewpoints for the synthesis of a specific point and the choice of which of the pre-selected input viewpoints to use for each ray of that specific point.

The pre-selection of input viewpoints from all captured viewpoints is based on the assumption that the closer the captured viewpoints are to the synthesized viewpoint, the more accurate the sampling of the surroundings will be (i.e., the relative size of the objects). As a result, all viewpoints further than a certain distance are discarded from the input.

After selecting the most appropriate captured viewpoints, the synthesized image is created by comparing the deviation angles of these viewpoints for each ray (i.e., pixel). The two closest viewpoints are then blended together on a per-pixel basis, so that there are no abrupt edges between mosaic areas. The blending function is presented in more detail in Section 3.2.

3.1.3. 2-DoF Synthesis using Flow-based Blending

Using this basic 2-DoF synthesis with regular blending works fairly well as long as the real scene geometry corresponds roughly to the proxy sphere geometry. The basic shape of many rooms can be approximated by a sphere; however the objects within these rooms can diverge greatly from the proxy sphere. In these cases, ghosting and doubling artefacts become visible, such as areas appearing twice or not at all, or two areas overlapping inconsistently. This problem is exacerbated when the synthesized viewpoint is very close to an object, as is visualized in Figure 3.3a: In this example the synthesized viewpoint S (dotted outline) is very close to a detailed object whose geometry diverges significantly from the proxy sphere. In this case, the values of the points captured by the two viewpoints vp1 and vp2 differ (orange vs purple), and neither of them is the desired ground truth value (gray). In order to improve the result, an adapted variation of the flow-based blending method from Richardt et al.'s Megastereo [RPZSH13] is introduced. This method allows interpolation between two 360° viewpoints using optical flow. Figure 3.3b shows how the interpolation can be used to achieve a more accurate result: A new viewpoint vp1-2 is interpolated between vp1 and vp2such that the interpolated viewpoint is located on the ray in question³. This new viewpoint is then used for the texture lookup to create the synthesized image with the goal of improving the accuracy of the mapped point.





(a) Detailed areas where real geometry is very dif- (b) Interpolating between input viewpoints ferent from proxy geometry are problematic.

using optical flow may improve results.

Figure 3.3.: Introducing flow-based blending to improve accuracy.

³Positioning the interpolated viewpoint directly on the ray is only possible for rays that are on the 2D plane containing all the viewpoints. All other cases must be approximated.

Adapting Flow-based Blending in Megastereo for 1-DoF Interpolation of 360° Images

Megastereo [RPZSH13] aims to generate high-resolution stereo panoramas by combining images captured on a circle. Their approach is to combine corresponding strips of the captured images and to create a view for each eye (see Section 2.2.2). In order to mitigate artefacts such as ghosting, they use "flow-based blending" to combine two images A and B, captured at viewpoints **A** and **B**. The optical flow vectors $F_{A\to B}$ and their inverse $F_{B\to A}$ are used for interpolation: To get the interpolated image S at position δ between viewpoints **A** and **B**, first, image A is morphed using Equation (3.1), which shifts each pixel x by distance δ along the optical flow vector $F_{A\to B}$. Then, image B is morphed using Equation (3.2), which does the same using the inverse optical flow and the distance $(1 - \delta)$. Then, the resulting shifted images I_A and I_B are blended using Equation (3.3). A demonstration of this operation on a pair of example images is shown in Figure A.1 on page 94.

$$I_A(x) = A(x + \delta \cdot F_{A \to B}) \tag{3.1}$$

$$I_B(x) = B(x + (1 - \delta) \cdot F_{B \to A}) \tag{3.2}$$

$$S = (1 - \delta) \cdot I_A + \delta \cdot I_B \tag{3.3}$$

The flow-based blending in Megastereo operates on planar images. In order to use it for 360° synthesis, it is necessary to adapt the method for 360° images.

A 360° image can be projected in several ways, as described in Section 2.1.1. The output of these projections is a planar image, meaning that it would be possible to apply flow-based blending directly. However, optical flow algorithms are generally designed to handle planar images without seams or distortions and would most likely produce unexpected results if used naively on planar projections of 360° images. As a result, the 360° images must first be projected and adapted in such a way that optical flow can be calculated accurately on them.

Of the projections presented in Section 2.1.1, only the cube map representation is applicable. Spherical representations are impractical, as aligning seams is not feasible and the distortion towards the edges is extreme. The latlong representation has only four seams to handle, but also distorts the image greatly around the poles. The cube map representation contains a number of seams but does not distort the image more than a planar image would. The challenge presented by the many seams of the cube map is to be able to track the points that move across the seams created by the six faces. Figure 3.4 shows an example of different points moving across seams, illustrating why calculating optical flow on each face separately would not be enough to track the points moving across the seams. Figure 3.4 also shows the linear discontinuities at the seams (e.g., at the upper edge of the carpet): Since each cube face is captured by a different virtual camera, angles are not consistent across seams. As a result, it is not possible to use the cube map as it is, since the optical flow assumes linear movement⁴.

To solve this problem, an *extended* cube map is introduced, which is also used by Huang et al. [HCCJ17] and Kolhatkar et al. [KL10] to adapt 360° images for structure-from-motion and optical flow algorithms, respectively. Instead of projecting a field of view of 90° for each camera, which covers exactly 360° of the image, the extended cube map uses a larger

⁴Optical flow uses vectors to describe movement, which are inherently linear


(a) Viewpoint **A** in cube map representation $(90^{\circ} \text{ FoV per face})$



Figure 3.4.: Points in the scene moving across seam edges need to be tracked by optical flow (the back face of the cube map is omitted for simplicity's sake)



(a) Viewpoint **A** in extended cube map representation (150° FoV per face)

(b) Viewpoint **B** in extended cube map representation $(150^{\circ} \text{ FoV per face})$

Figure 3.5.: Points that traversed a seam in the regular cube map can be tracked across the original seams in the extended cube map

field of view for each camera (in this case, 150°). Consequently, some areas of the scene are represented several times, since the areas of the image that are near a seam are represented on each face that is adjacent to the seam. This way, when calculating optical flow on each face separately, points that move across where the seam would be in a regular cube map remain on the face with the corresponding projection. Figure 3.5 shows the front, top, and left faces of the extended cube map representation of the cube map shown in Figure 3.4. In the extended cube map, the tracked points do not traverse a seam on any of the faces, meaning optical flow can be calculated on the entire original face.

Nonetheless, this method is still limited by the field of view used by the virtual cameras. If the maximum displacement is larger than the face extension, the extended cube map will not be sufficient, as the points can also traverse the extended seams. Also, the larger the field of view, the more the image will be distorted towards the edges of a face, which may lead to distorted optical flow results. Both problems are visible in Figure 3.5: The lamp in the left face has such a large displacement between Figure 3.5a and Figure 3.5b that it is partly cut off in Figure 3.5b. On top of being cut off, it is also greatly distorted, which will result in distorted optical flow values for that area.

In general, this means that displacement between two images is limited. However, the displacement that is trackable by optical flow algorithms is also limited. The effect of these limitations will be explored in Chapter 4.

Despite these limitations, using the extended cube map makes it possible to calculate optical flow on each face separately, meaning that Megastereo's flow-based blending method can be applied to two 360° viewpoints **A** and **B**: First, the extended cube map projections A_{ext} and B_{ext} are created from the image data. From this point, each set of faces A_{ext}^i and B_{ext}^i , $i \in [top, left, front, right, bottom, back]$ is handled separately. Optical flow $F_{A\to B}^i$ and inverse optical flow $F_{B\to A}^i$ are calculated for A_{ext}^i and B_{ext}^i . Then, the interpolated extended image is calculated using Equation (3.3). Finally, for each face, the extended parts of the extended cube map are clipped so that each face once again has a field of view of 90°, resulting in the interpolated 360° image at position δ between viewpoints **A** and **B**. Since the flow-based blending method is applied to two complete images instead of image strips like in Megastereo, it is equivalent to interpolated viewpoint can then be used for texture lookup just like a captured viewpoint.

2-DoF Synthesis with Flow-based Blending

Adapting Megastereo's flow-based blending for 1-DoF interpolation of 360° images allows the creation of a new viewpoint between **A** and **B** that is closer to the actual ray (Figure 3.3b). In order to leverage this to improve the basic 2-DoF synthesis, the 1-DoF interpolation needs to be integrated in the 2-DoF synthesis algorithm. For each pixel of the synthesized image, a set of input viewpoints **A** and **B** needs to be chosen for use in the 1-DoF interpolation. Then, based on the positions of **A** and **B**, and the ray in question, an interpolation distance δ must be calculated that defines the position of the 1-DoF interpolation between **A** and **B**.

For these steps, an approximation needs to be made due to the 2-DoF restriction: Figure 3.6a and Figure 3.6b show the ideal case, where the target point T is on the same horizontal plane as the captured points and the synthesized point (the viewpoint plane). In this case, there are a number of different positions directly on the ray that are also on the plane. Depending on the input viewpoints, the most convenient can be chosen and an



Figure 3.6.: Example of different target points in the scene



Figure 3.7.: Examples of the choice of viewpoints **A** and **B** for 1-DoF interpolation based on deviation angle and position on either side of the ray. The two sides of the ray are color coded in white and orange.

interpolated viewpoint calculated at that position. However, this is only the case for all target points on this plane. All other target points in the scene lie either above or below the viewpoint plane, for example in Figure 3.6c, where T is above the plane. In these cases, the only intersection of the ray and the viewpoint plane is at the synthesized viewpoint. Finding the set of viewpoints **A** and **B** that allow the closest 1-DoF interpolation to this point is not trivial, as it would require comparing the minimum distance of the point to all vectors between all the possible sets of viewpoints. In order to simplify this problem, all the rays that are not on the viewpoint plane are approximated.

To approximate a ray pointing at target point T at the spherical coordinates (r, θ, φ) , the elevation θ is reduced to 0, assigning the spherical coordinates to $(r, 0, \varphi)$, which is equivalent to moving T to the viewpoint plane by the shortest path. This will yield less accurate results as the actual ray moves towards the poles, since the deviation angle between the actual ray and the approximated ray increases towards the poles. However, this approximation is computationally and mathematically much simpler and should yield acceptable results.

With this approximation, the viewpoints \mathbf{A} and \mathbf{B} used for 1-DoF interpolation can be

chosen. As in the 2-DoF synthesis with regular blending, the metric for choosing **A** and **B** is the deviation angle. The actual rays, not the approximated rays, are used for the calculation and comparison of the deviation angles, since there is no need to use the approximated rays at this point. However, for the choice of **A** and **B**, an additional constraint is included: The two viewpoints chosen must be *on either side* of the approximated ray, so that there is an intersection between the vector connecting the viewpoints **A** and **B** and the approximated ray. Figure 3.7 shows three different examples of the selection of viewpoints **A** and **B**: In Figure 3.7a, the viewpoints vp1 and vp2 are chosen, because they are on either side of the ray in question (visualized by white and orange hemispheres) and they have smaller deviation angles than vp3 and vp4. In Figure 3.7b, vp3 and vp1 are chosen, and in Figure 3.7c, vp1 and vp4 are chosen.

Once the viewpoints \mathbf{A} and \mathbf{B} are chosen for each target point T , the interpolation distance $\delta \in [0, 1]$ is calculated, which is the point on the vector $\overrightarrow{\mathbf{AB}}$ that intersects the approximated ray. The calculation of δ is a simple line intersection calculation, explained in Section 3.2.

Using the chosen viewpoints **A** and **B**, and the calculated interpolation distance δ , a 1-DoF interpolation is calculated for each approximated ray. Using this interpolated viewpoint, a texture lookup is then performed for each pixel associated with that ray. This results in a mosaicked image where each image area is an interpolated, reprojected viewpoint. The 1-DoF interpolation step should improve some of the artefacts caused by the use of the proxy sphere instead of the actual scene geometry. Its effectiveness and limitations are explored in Chapter 4.

3.2. Implementation Details

This section presents the technical and mathematical details on which the 2-DoF synthesis with regular blending and the 2-DoF synthesis with flow-based blending are based. Both methods are implemented in Python3 [Pyt18], using the libraries NumPy [The19b], OpenCV [The19a], SciPy [The20], and scikit-image [vdWSN⁺14]. For the conversion between different 360° projections, as well as the calculation of the extended cube map, the library "skylibs" [Hol20] is used. The implementation code can be found on Github⁵.

The synthesis process is shown in Figure 3.8: The captured data, which is encapsulated in the CaptureSet class, is passed to the *2DoFSynthesizer*, along with the desired location of the viewpoint to be synthesized. Using this data, the input viewpoints are selected, and passed on for ray-sphere intersection and deviation angle calculation. Then, depending on whether regular blending, or flow-based blending is used, the blending is performed using the results of the previous step, which produces the synthesized image.

First, the preprocessing step in which the captured data is prepared for synthesis is described (Section 3.2.1). Then, the details of the implementation of the synthesis process with regular blending are presented, including the deviation angle calculation (Section 3.2.2), followed by the details of the synthesis with flow-based blending (Section 3.2.3).

3.2.1. Preprocessing

The input data consists of a set of captured images in latlong representation, a text file containing the metadata (positions and orientations) of these viewpoints, and the approximate

⁵https://github.com/rskletza/360imageSynthesis



Figure 3.8.: System diagram of the 2DoFSynthesizer

scene radius. In order to easily and intuitively access the locations and image data of the captured viewpoints, the data is encapsulated in the CaptureSet class. The CaptureSet class first parses the metadata; then, with this information, rotates all the images so that they have the same orientation, and shifts the viewpoints so that they are centered around the origin (0,0,0). This is done under the assumption that images were captured in a regular distribution throughout the room. The proxy sphere representing the scene is also centered at the origin. Instead of storing the image data directly in the CaptureSet, the file paths are stored so that the images can be dynamically loaded when needed. The CaptureSet can then be used by the 2DoFSynthesizer to synthesize a new image either using regular blending or flow-based blending at any given location within the scene⁶.

3.2.2. Basic 2-DoF Synthesis using Regular Blending

For the basic 2-DoF Synthesis, the steps described in detail in this section are the selection of input viewpoints, the calculation of the ray-scene intersections and deviation angles, as well as the blending function introduced in Section 3.1.2 and the texture lookup which reprojects the captured viewpoints.

Selecting Appropriate Input Viewpoints

Before calculating ray-scene intersections and performing texture lookup, the most appropriate input viewpoints are selected from the complete set of input viewpoints. The weighting function that blends different captured viewpoints together (introduced in Section 3.1.3) does not factor in the euclidean distance, relying only on the deviation angle. However, the euclidean distance has an impact on the accuracy of the resampling, in that captured viewpoints that have a large euclidean distance from the synthesized viewpoint will not necessarily yield the "correct" value due to different sampling rates during image capture. For example, if one viewpoint is very close to a door, the doorknob may be represented by a large number of pixels, accurately depicting its outlines and reflections. Another viewpoint that is at the other end of the room, but in the same line of sight might represent the same doorknob with only a very small number of pixels, losing information on the exact outline and reflections. Even though the deviation angle between these two viewpoints may be zero, the pixels representing the image area are not identical. As a result, the captured viewpoints

⁶Given that it is within the convex hull of the captured viewpoints

are filtered before synthesis. All viewpoints outside a certain radius are discarded. The radius is chosen dependent on the scene size and the density of captured viewpoints. If the set of viewpoints within the radius is empty, all viewpoints are used, regardless of distance.

Calculating Ray-sphere Intersection

The ray-sphere intersection is used in the raytracing-based texture lookup to find the scene points captured by the synthesized viewpoint (see Figure 3.1c). This raytracing process is a basic raytracing technique used in computer graphics. First, it is necessary to retrieve the vector representing the ray, in order to calculate the intersection of a ray with the proxy sphere. These vectors can be easily derived from the unit directions of the 360° image at any viewpoint (see Section 2.1.1): Each unit direction is a vector on the unit sphere, representing the location of an image value (pixel). These coordinates are in *model space*, meaning that they are centered around zero. Translating them into *world space* moves the rays to their respective location in the scene. From this location, the rays represented by the vectors are cast into the scene, where they will intersect with the proxy geometry.

The intersections of these rays with the proxy sphere geometry can be calculated analytically: The proxy sphere, which is centered at the origin, can be represented implicitly by Equation (3.4). A point P representing any point on the surface of the sphere is defined by Equation (3.5). Equation (3.6) describes any point on the ray, where O is the origin of the ray, which is the center of projection of the new viewpoint, t is the length of the ray and Dis a unit vector representing the direction.

$$x^2 + y^2 + z^2 - R^2 = 0 aga{3.4}$$

$$P^2 - R^2 = 0 (3.5)$$

$$P = O + tD \tag{3.6}$$

The point P in Equation (3.5) can be substituted with Equation (3.6) which yields Equation (3.7). This equation can be developed into Equation (3.8), which is a quadratic function with $a = D^2$, b = 2OD, $c = O^2 - R^2$, shown in Equation (3.9).

$$(O+tD)^2 - R^2 = 0 (3.7)$$

$$D^2 t^2 + 2ODt + O^2 - R^2 = 0 (3.8)$$

$$a = D^2, b = 2OD, c = O^2 - R^2$$

 $f(t) = at^2 + bt + c$ (3.9)

$$t = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$
(3.10)

This equation can then be solved for t. Since the radius of the sphere is chosen so that it contains the complete scene and no viewpoints are synthesized outside of the scene, the quadratic function will always have two solutions (i.e., two intersections): one for which the



(a) The deviation angles of one input viewpoint in latlong format



(b) The stacked deviation angles of all input viewpoints

Figure 3.9.: Visualization of deviation angle storage

vector sign is negative, and one for which the vector sign is positive. Since the original ray used for the calculation is unidirectional (i.e., it cannot invert its direction), it needs to be extended by a positive value. The original ray, being a unit ray of length 1, can then be multiplied by the positive t, which yields the intersection point.

The vectors and intersection points are each calculated and stored in latlong representation (i.e., a matrix of vectors of the same shape as the latlong image), which means that they can easily be associated with the unit directions, as well as the uv coordinates (and thus, pixel values) using the latlong mapping function. By storing the values in this representation (i.e., 3D matrix), Numpy's vectorization can be used, which greatly facilitates implementation.

Deviation Angle Calculation

The deviation angle calculation is a simple angle calculation between two rays (i.e., vectors). The rays are defined by their origin (location of the viewpoint, both captured and synthesized), and the intersection points calculated in the previous step. The deviation angle calculation is performed for each ray of the synthesized point and the corresponding rays of all N input viewpoints, which results in N deviation angles per ray of the synthesized point. Figure 3.9a depicts how the deviation angles between the synthesized viewpoint and a single captured viewpoint are stored: Each field $\alpha_{x,y}$ contains a deviation angle α associated with the ray at the same position. The deviation angles for all captured viewpoints are stacked in a three-dimensional matrix, shown in Figure 3.9b, which allows comparison of the deviation angles per pixel/ray of all the viewpoints in the next steps.

"Regular" Knn Blending

The previously calculated and stored deviation angles are used for the regular blending step. The storage of the deviation angles in the three dimensional matrix (Figure 3.9b) makes the selection of the best viewpoint per pixel very straightforward, since the ID of the k best input viewpoints (i.e., with the smallest deviation angles) can easily be extracted using *numpy.argmin* and the corresponding pixel value retrieved from the captured viewpoint corresponding to the ID. With this information, the "regular", k-nearest-neighbor (knn) blending is performed.

The regular blending function combines the values of the rays of the k closest deviation angles α . The idea is to weight deviation angles of 0 very highly and all larger deviation



Figure 3.10.: The inverse sigmoid function used for weighting



Figure 3.11.: K-nearest-neighbor blending with different values for k. The images are clipped from the latlong representation of an image synthesized using regular blending.

angles with exponentially low values. This is done with an inverse sigmoid function (Equation (3.11), visualized in Figure 3.10). The parameters of the function were found by trial and error.

$$w(\alpha) = \frac{1}{(1 + e^{500 \cdot (\alpha - 0.017)})}$$
(3.11)

After calculating w for the k best viewpoints, the per-pixel weights w are normalized so that their sum for each pixel is one. In this way, the final image is not oversaturated. Blending the k best viewpoints per pixel results in smoother transitions between the mosaicked areas. Figure 3.11 shows the difference between using k = 1 and k = 2: It is clearly visible that the border between two mosaicked areas (e.g., on the rug in the center of the room) is very abrupt in Figure 3.11a, because the two areas do not align perfectly. This border is much smoother in Figure 3.11b, since the two areas are gradually blended into one another. Using k > 2 does not have much impact, since most deviation angles where k > 3 are too large to have an effect. As a result, k is chosen to be 2 for the regular blending implementation.



space in model space (b) The normalized rays $\Gamma_i - V$ (c) The result of resampling based on uv coordinates

Figure 3.12.: Texture lookup by uv remapping

Texture Lookup

Finally, using the viewpoints selected through the deviation angles, the texture lookup shown in Figure 3.1d-f is performed by resampling using uv coordinates. Given a captured viewpoint at the location V and the ray-scene intersections ("targets") T_i from the synthesized viewpoint, where i denotes which ray is being examined, the rays from V to the targets can easily be calculated by $T_i - V$, shown in Figure 3.12a. These rays are then normalized to have length 1 and returned to model space, shown in Figure 3.12b. The normalized rays in model space are in the same format as the unit directions and can therefore be transformed to image coordinates using the latlong mapping function (see Section 2.1.1), implemented in the library Skylibs [Hol20]. These image coordinates (i.e., uv coordinates) can be used to resample the data, which is equivalent to actually performing a ray-by-ray texture lookup. The result of the resampling along with the "new" rays is shown in Figure 3.12c. This resampling based on uv coordinates is also implemented in Skylibs and utilizes Scipy's function *scipy.ndimage.map_coordinates*.

Finally, the pixel values of the different remapped viewpoints are multiplied by the normalized weights associated with that viewpoint and the weighted latlong images are added up to give the final synthesized image.

3.2.3. Flow-based Blending

The 2-DoF synthesis with flow-based blending also utilizes the ray-sphere intersection, the deviation angle calculation and the texture mapping. The details of the flow-based blending steps, i.e., the input viewpoint selection, the choice of viewpoints **A** and **B** for the 1-DoF interpolation, the calculation of the interpolation distance δ , as well as the 1-DoF interpolation are explained in this section.

Selecting Appropriate Input Viewpoints

The adaptation of optical flow algorithms for 360° images, as well as most optical flow algorithms themselves, are limited to a maximum displacement. This is not considered in the algorithm itself, so it is handled in the input viewpoint selection. The goal of the input selection is to find a minimal convex hull around the point to be synthesized from the set of captured viewpoints. If there is at least one captured viewpoint in each quadrant around

the synthesized viewpoint, then the closest point from each quadrant is selected. If there is no point in one of the quadrants, the points in the quadrants adjacent to the empty quadrant are selected so that they are as close to the empty quadrant as possible. Since the synthesized point is in the convex hull of all the captured points, there must exist a solution for the minimal convex hull. In the worst case, the minimal convex hull is so large that the optical flow algorithm fails.

Choosing the Viewpoints A and B

The 1-DoF interpolation requires that the two input viewpoints **A** and **B** are chosen so that they are on either side of the ray in question (see Figure 3.7), so that the line on which the images can be interpolated intersects the approximated ray. Since all the viewpoints are on a plane, the "side" a viewpoint is on is defined by whether the deviation angle is between 0 and 180° (one side) or between 180° and 360° (other side). To get the best deviation angles on either side, the viewpoints with angles closest to 0° and closest to 360° are chosen.

The only problem with this process would arise if there was no viewpoint on the other side of the axis. However, because of the restriction that all synthesized points must be within the convex hull of the captured points, this can never happen. In the worst case scenario, there is only one viewpoint on the other side of the axis with a very large deviation angle. This is acceptable, since this viewpoint is not directly used, instead the 1-DoF interpolation creates a new viewpoint with an ideally very small deviation angle.

Determining the 1-DoF Interpolation Distance δ

Given the two viewpoints **A** and **B**, it is now possible to calculate the intersection of \mathbf{AB} and the approximated ray (elevation $\theta = 0$) between the synthesized point **S** and the target point **T** in the scene. Figure 3.13 shows how this process enables the interpolation of a viewpoint with a small deviation angle (zero, if **T** is on the viewpoint plane): The 1-DoF interpolation can interpolate a point on the line between viewpoints **A** and **B**, which can be chosen so that it intersects the ray between **S** and **T**. The interpolated viewpoint should yield a more accurate result than both **A** and **B** (first introduced in Figure 3.3). The calculation of the intersection between two lines is a method from [Col]. Using these four points **A**, **B**, **T** and **S**, two infinite lines can be defined by Equation (3.12). The intersection point at $d \cdot \overrightarrow{AB}$ is given by Equation (3.13), where x_P/y_P represent the x/y coordinates of point $P \in [\mathbf{A}, \mathbf{B}, \mathsf{T}, \mathsf{S}]$

$$\overrightarrow{\mathbf{AB}} = \mathbf{A} + d \cdot (\mathbf{B} - \mathbf{A}) \qquad \overrightarrow{\mathsf{ST}} = \mathsf{S} + u \cdot (\mathsf{T} - \mathsf{S}) \tag{3.12}$$

$$d = \frac{(x_{\mathbf{A}} - x_{\mathbf{S}})(y_{\mathbf{S}} - y_{\mathbf{T}}) - (y_{\mathbf{A}} - y_{\mathbf{S}})(x_{\mathbf{S}} - x_{\mathbf{T}})}{(x_{\mathbf{A}} - x_{\mathbf{B}})(y_{\mathbf{S}} - y_{\mathbf{T}}) - (y_{\mathbf{A}} - y_{\mathbf{B}})(x_{\mathbf{S}} - x_{\mathbf{T}})}$$
(3.13)

Since the synthesized viewpoint S is within the convex hull, there is always an intersection $d \in [0, 1]$. This value can then directly be used as δ . The only case that merits an exception is if the synthesized viewpoint is directly on the border of the convex hull, i.e., directly on the line between two captured viewpoints. In this case, the ray that is parallel to vector \overrightarrow{AB} is equal to the line \overrightarrow{AB} . As a result d is not defined and δ must be found by dividing the distance $|\overrightarrow{AS}|$ by $|\overrightarrow{AB}|$.



Figure 3.13.: A different δ is calculated based on the intersection of \overrightarrow{AB} and \overrightarrow{ST} , in order to interpolate a new viewpoint at the interpolation distance δ between viewpoints **A** and **B** with an identical line of sight to **T** as \overrightarrow{ST} .

1-DoF Interpolation

Given the two viewpoints **A** and **B** and the interpolation distance δ , the interpolated image at δ between **A** and **B** can be calculated. The different steps in the process are: extending the cube map, calculating optical flow on the extended cube map, interpolating the images using the optical flow, and transforming the interpolated, extended cube map back into latlong representation so that it can be remapped in order to be used for blending.

Extended Cube Map The class *ExtendedCubeMap* uses the 360° image data and the virtual camera provided by skylibs [Hol20] to "extend" the cube map by capturing a virtual image for each face of the cube with a 150° field of view. This is done for both viewpoints **A** and **B**. The *ExtendedCubeMap* class handles the extended faces and can perform different functions on them, such as the optical flow calculation, which is required for the next step.

Optical Flow Calculation and Image Shifting The optical flow algorithm used in the implementation is Farnebäck's algorithm implemented by OpenCV (cv2.calcOpticalFlowFarneback) [The19a]. For calculating optical flow between two ExtendedCubeMaps **A** and **B**, the ExtendedCubeMap class provides a function $optical_flow$, which takes as arguments the optical flow algorithm, and a second ExtendedCubeMap to use for optical flow calculation. Passing the optical flow function dynamically greatly simplifies exchanging the optical flow algorithm for future work.

The ExtendedCubeMap then calculates the optical flow separately between each corresponding pair of extended faces. On top of the optical flow from ExtendedCubeMaps A to B, the inverse optical flow from ExtendedCubeMaps B to A is required as well. The inversion of optical flow is nontrivial, since inverting the optical flow vectors is not enough: In order to calculate the inverse optical flow field, the original optical flow field must first be shifted by its own vectors and then inverted: For example, a vector (1,3) at position (10,10) in the optical flow field must be shifted to position (10+1, 10+3) and then reversed to (-1, -3). Alternatively, the optical flow can just be calculated on the ExtendedCubeMaps in reverse, i.e., from B to A. This is the option is used in the proof-of-concept implementation.

Using the optical flow, the inverted optical flow, and the interpolation distance δ , the

shifted images $I_{\mathbf{A}}$ and $I_{\mathbf{B}}$ are calculated separately for each face by using Scipy's *scipy.ndimage. map_coordinates*, with image coordinates shifted by the optical flow vectors and δ , and the inverse optical flow vectors and $(1 - \delta)$, respectively. The shifted *ExtendedCubeMap* images $I_{\mathbf{A}}$ and $I_{\mathbf{B}}$ are then combined using Equation (3.3). The result is an interpolated *Extended-CubeMap* at interpolation distance δ .

Before passing this on to the blending step of the 2-DoF synthesis, the *ExtendedCubeMap* is transformed back into a regular cube map by clipping each face back to its original size and reprojecting the cube map back to a latlong map, since all other processing steps use the latlong format.

Flow-based Blending

The flow-based blending step combines all of the previous steps: First, for each ray, of the synthesized image, the viewpoints **A** and **B** are selected and the interpolation distance δ is calculated. Then, a mask is created for each set (**A**, **B**, δ), masking all pixels that do not belong to the set, and the interpolated image for that set is calculated and reprojected to the location of the synthesized viewpoint using texture lookup. This is repeated for all sets.

The complexity of the flow-based blending is directly bound to the precision of δ . Given a precision of two decimal points results in 101 different interpolated images ($\delta \in [0.00, 0.01, 0.02 \dots 0.99, 1.00]$), whereas precision of one decimal point results in only 11 interpolated images. A precision of two decimal points is used in the implementation, since this is an acceptable compromise between complexity and a result with smoother transitions.

Finally, the masked interpolated latlong images are added together to give the final result.

3.2.4. Performance

As this is a first attempt at 2-DoF synthesis, performance is not deemed important, and no parallelizations are incorporated. Since the algorithms operate in a pixel-wise fashion, the computation time increases exponentially for larger image resolutions ($O(n^2)$ complexity). The performance of the flow-based blending depends on the location of the synthesized point in relation to the captured points. In the worst case, one interpolated image must be calculated per pixel, at best one interpolated image must be calculated for the whole image (if a synthesized viewpoint is directly on a line between two captured viewpoints). The non-optimized interpolation of a whole image for pixel regions (and in the worst case, single pixels), makes the flow-based blending significantly slower than the regular blending.

The synthesis of an image of 1000x500 pixels in latlong representation with no optimization using regular blending with 4 input viewpoints takes approximately 4s on a single Intel Xeon (Skylake) processor, whereas flow-based blending with the same input takes between 10 and 30 minutes, depending on the constellation of the viewpoints. Fortunately, many of the operations are "embarrassingly parallel", meaning they can be very easily parallelized in the future.

Unfortunately, there are no publicly available benchmarks for 360° image synthesis with 2-DoF without 3D geometry, as not many methods exist that try to achieve this. This chapter presents an evaluation of the approach presented in Chapter 3, relying on mathematically calculable error metrics. These metrics measure the accuracy of a synthesized image compared to the ground truth and are used to assess the effect of a limited number of parameters. Using these metrics, it is possible to measure the performance of the 2-DoF synthesis using regular blending, and the 2-DoF synthesis using flow-based blending and compare the two. Performance in the context of this evaluation is defined as the accuracy of the synthesized image based on the error metrics, as well as visual examination.

In order to understand the evaluation process, possible parameters of the algorithm and of the scene are discussed (Section 4.1), followed by the presentation of the evaluation methodology (Section 4.2). Then, virtually generated scenes are used to evaluate the effect of different combinations of select parameters in a controlled environment (Section 4.3). Based on the knowledge gained in the parameter evaluation, a proof-of-concept evaluation is performed on a real scene (Section 4.4). Finally, the limitations of the evaluation are discussed (Section 4.5).

4.1. Parameters

Before defining the parameters to test in the parameter evaluation, this section gives an overview of possible parameters in the context of the 2-DoF algorithm presented in Chapter 3. The 2-DoF algorithm already makes a few assumptions, for example the constraint to the viewpoint plane, the fact that the scene is static, and more (stated in Section 3.1). These assumptions are upheld in the evaluation, as they are prerequisite to the algorithm.

The remaining parameters that are not constrained by the assumptions can be divided into two categories:

- **Internal parameters** i.e., parameters based within the algorithm, such as the blending type and the selection of input viewpoints.
- **External parameters** i.e., parameters based on the properties of the captured scene, such as the viewpoint density, or the geometry of the scene.

The internal parameters can be modified after the scene has been captured, the external ones cannot. The most prominent internal parameters based on the implementation from Chapter 3 are:

- location of synthesized points within the scene (near walls, objects, etc)
- location of synthesized points relative to the captured points
- blending type, i.e., flow-based blending or regular blending

• optical flow algorithm used for flow-based blending

There are more internal parameters that could theoretically be modified, such as the knn blending function (Equation (3.11)), or the method of ray approximation for 2-DoF in the flow-based blending algorithm (Section 3.1.3), but these will be assumed immutable for this evaluation, as the variation of these parameters would require developing new functions, which is outside the scope of this thesis.

As for the possible external parameters, the number of different possible scenes is infinite, but the assumed key parameters are:

- type of scene (outdoor, indoor, etc) \rightarrow size and general shape of the scene
- objects within the scene
- density and distribution of captured viewpoints

External parameters such as the camera settings (e.g., aperture, shutter speed, white balance) and the lighting throughout the scene are not considered; it is assumed that all the captures have the same camera settings and white balance parameters. Furthermore, the evaluation is restricted to indoor scenes of approximately $25m^2$. This reduces the parameter space significantly, since indoor scenes tend to be enclosed by walls, which enforces a maximum distance of objects to the camera. Scenes where there is no enforced maximum distance of objects to the camera, (e.g., outdoor scenes with a large distance of objects to the viewpoints) are less relevant for this evaluation, since the geometry of such outdoor scenes can be generalized as a sphere or a cube, an effect which is often used to decrease render time in video games¹. In smaller scenes, the difference between the scene and proxy geometry can lead to artefacts, which makes these scenes more appropriate for the comparison between flow-based blending and regular blending.

The evaluation presented in this thesis aims to examine the effects of a few select internal and external parameters, instead of exhaustively examining all of them. In order to do this, a *scenario* is designed for each selected parameter. The scenario attempts to demonstrate the effect of this parameter on the accuracy of the result. It must be noted that limiting the evaluation to specific scenarios reduces the testing space but might also lead to missing some interactions between parameters.

4.2. Evaluation Methodology

The evaluation is divided into two distinct phases: a parameter evaluation using virtual scenes, and a proof-of-concept evaluation using real scenes. Both evaluations follow the approach depicted in Figure 4.1, which consists of four steps, depicted from left to right: *scenario definition*, where a scenario is designed to test a specific parameter using static and dynamic parameters and a captured scene, *synthesis*, where the synthesized images are calculated using the 2-DoF synthesis algorithms presented in Chapter 3 as well as a naïve algorithm as a baseline, *error calculation*, where the accuracy of the synthesized images is measured using mathematical error metrics, and *result analysis*, where the cause and effect of the parameters is examined in several stages. The details of each step of the evaluation, from left to right in Figure 4.1, are described in the following sections.

¹referred to as a "skybox" or a "skydome", respectively



Figure 4.1.: Methodical approach for the evaluation of a scenario

Scenario Definition

The scenario definition is the first step of the methodical approach depicted in Figure 4.1. A scenario is defined by the parameter that it tests, the static parameters that are used, and the scene where the data was captured. Although a scenario is designed to test a specific parameter, which then is "dynamic" (i.e., will be modified throughout the scenario), there might also be more dynamic parameters. For example, in a scenario for exploring viewpoint density, the blending type is also modified to see what effect the viewpoint density has on regular and flow-based blending. The static parameters include the location of the synthesized viewpoints and any other parameter that remains unchanged throughout the scenario is tested on. Although the scene is part of the parameters (the external parameters, to be exact), it merits particular mention, as it contains the actual image data that is used for synthesis. This data, along with the other parameters defined in the scenario, is then passed on to the synthesis step, shown as the output of the scenario definition step in Figure 4.1.

Synthesis

The synthesis step consists of three parts: the 2-DoF synthesis presented in Chapter 3 using regular blending and flow-based blending, and a baseline synthesis using a naïve algorithm. The naïve algorithm consists of simply selecting the nearest neighbor viewpoint based on euclidean distance. The results of the naïve algorithm serve as a baseline comparison to verify whether the developed 2-DoF algorithm is an improvement to a naïve approach. If either the regular or the flow-based blending generally performs worse than the naïve algorithm, this is an indication of a substantial flaw in the approach. After synthesizing the images using all three algorithms with identical input parameters, the resulting images are passed on to the error calculation.

Error Calculation

There are many properties that a synthesis algorithm can be evaluated for, for example execution speed, visual acceptability (based on user studies), number of artefacts, or distance from the ground truth. In this evaluation, mathematical error metrics are used to compare each result to its ground truth image, which needs to be captured beforehand. Two metrics, the L1 error and the SSIM error, are chosen since they are based on different image features. By using two different metrics, potential limitations of each metric can be compensated for by the other. However, it must be taken into account that neither metric is designed specifically for the task of measuring accuracy of 360° synthesized images. As a result, it is necessary to monitor and verify their results by visual examination, especially in cases where the results do not correspond. The details of the L1 and SSIM error metrics are presentented in the following sections.

L1 error on RGB The first metric is the L1 error, which is calculated between the ground truth image and the synthesized image in RGB color space. This error metric calculates the mean absolute difference of the RGB values and therefore indicates the mean accuracy of each pixel of the image. Equation (4.1) shows the formula for the L1 error metric: The difference of the RGB color values $r, g, b \in [0, 1]$ (for floating point values) is calculated for each pixel of the ground truth (P^{gt}) and synthesized (P^s) images, then all of the differences are added together, and divided by the number of pixels (P) in the image. The range of error values is $e_{L1} \in [0, 3]$.

$$e_{L1} = \frac{1}{|P|} \cdot \sum_{r}^{P} |(P_r^{gt} - P_r^s)| + |(P_g^{gt} - P_g^s)| + |(P_b^{gt} - P_b^s)|$$
(4.1)

A visualization of the L1 error can also be created by calculating the sum of absolute differences per pixel without averaging the values. Figure 4.2c shows an example visualization of the L1 error between the two images Figure 4.2a and Figure 4.2b. The error visualization in Figure 4.2c shows the errors per pixel by encoding areas of the image where there is a very large difference with a value closer to white and areas where there is no difference as black, which highlights areas of the image that are problematic. For example, the area where the blue rug overlaps in Figure 4.2a and Figure 4.2b is black, whereas the area where it does not is white. Since the sum of the differences between all three color values is used, the visualization can contain oversaturated white areas where the pixel value is larger than 1. Although some information on the severity of the error values is lost due to the oversaturation, problematic areas are more easily recognizable, which is more important for this evaluation.

The L1 error is useful because it gives a rough estimate of how accurately each pixel is synthesized. The visualization indicates in which areas the synthesized image is inaccurate, which is helpful for classifying problems. However, a drawback of the L1 error is that it relies on color values, so images with large differences in pixel values will generally produce a higher error value than images with smaller differences in pixel values, even though the distortion and displacement may be the same.

As in the case of optical flow calculation, some adjustment must be made to adapt this metric for 360° images. Since the latlong representation is not equal-area, the areas towards



Figure 4.2.: Example visualization of L1 RGB error. The error values are oversaturated, which makes them more visible.

the poles would intrinsically have a higher weighting, since L1 is calculated per pixel. To avoid this problem, the cube map representation is used, since it does not significantly distort the image. The average value is then calculated using the six faces of the cube.

SSIM error on Grayscale The metric to complement the L1 error is a variation of the structural similarity index (SSIM) [ZBSS04], which measures the *structural similarity* between two images. Instead of comparing the images pixel by pixel, the SSIM uses the luminance, contrast and structure of the images for comparison. It compares these locally, i.e., it operates on smaller areas instead of the image as a whole. Consequently, it is possible that the SSIM does not register small displacements in the scene if the objects are not distorted. However, the additional comparison with the L1 error should mitigate this potential problem.

The SSIM metric in general, and the implementation used in this evaluation² return a value $SSIM \in [-1, 1]$ with 1 signifying an extremely similar image and -1 signifying a very different image. In order to be able to compare it more easily with the L1 error, the SSIM value is converted to an error value $e_{SSIM} \in [0, 1]$, with 0 signifying an identical image with no error and 1 signifying a very different image.

The SSIM error is calculated on the grayscale image in cube map representation. There is no need to use an RGB image, since it does not use color values. The cube map representation is again used to avoid possible problems with distortion.

Result Analysis

After calculating the error metrics of all of the synthesized images, the results are analyzed. For each scenario, the number of results depends on the number of tested parameters and the number of synthesized viewpoints. Furthermore, for each synthesized image, there are two error metrics to be considered. Altogether, this can lead to a very large number of results. In order to effectively analyze this potentially very large number of results, it is necessary to break the analysis down by creating different visualizations that highlight different attributes of the results, depicted as the last step in Figure 4.1. At first, an overview is created using all the calculated error values e, the "distribution comparison". Using this visualization, interesting cases e^* are selected. These cases are examined in more detail using the "scene analysis" which shows the results in the context of the scene. Then, exemplary results e^*

²skimage.metrics.structural_similarity [vdWSN⁺14]



(a) Boxplot example for distribution comparison of the results of regular blending in the "square room"



(b) Visualization for scene analysis: The error values from the boxplot in (a) are mapped to colors at the positions of the viewpoints in the scene. Light green represents the worst value (0.268) and dark blue the best value (0.143).

Figure 4.3.: Different types of result visualizations for L1 error values for example results of regular blending in a scene

are again selected and the corresponding synthesized images are inspected visually in the "sample inspection". These analysis techniques and their corresponding visualizations are detailed in the following sections.

Distribution Comparison The first step of the analysis is a comparison of error value distribution. In order to compare all the error values of a scenario, the values are plotted using a boxplot. Figure 4.3a shows an example boxplot: The different parameter combinations of the scenario are plotted on the y axis (e.g., the scene "square room") and the error distribution (i.e., the error values of all the synthesized viewpoints) is plotted on the x axis. The box plot shows the distribution of these values: The thick black line in the colored box is the median value (approx. 0.177 in Figure 4.3a); the colored ranges to the left and right of the median describe the "interquartile range" (IQR), the range of the closest half of the data (25% on each side). The "whiskers" of the plot extend to the minimum and maximum of the values. The minimum and maximum are defined as $1.5 \cdot IQR$. Any data outside of the range between the minimum and the maximum, are the "outliers", depicted as small crosses. The boxplot gives a general overview of how the error values of the specific scene are distrubuted. The distribution of the error values of the results in Figure 4.3a, for example, shows that the first three quartiles of the results are fairly close to the median (between approx. 0.14 and 0.19), whereas the fourth quartile extends over almost the same range (0.19 to 0.225) and there are some extreme outliers. This indicates that there are some viewpoints with significantly worse values than most of the others.

Scene Analysis Based on the insights gained in the distribution comparison, the most interesting cases are selected for closer analysis. These cases are examined by color coding the error values and assigning the colors to the positions in the scene. This puts the error values in context with the scene surroundings. In the example distribution visualization in Figure 4.3a, there is only one scene, so the choice is trivial: Figure 4.3b shows the synthesized points in the context of this "square room" scene, color coded by their error values. The

maximum and minimum values of the points (visible in Figure 4.3a as the values furthest to the right and left, respectively) are coded as light green and dark blue, respectively. This visualization gives a more detailed overview over the values of the different points. In Figure 4.3b, for example, the synthesized points near the right wall of the room have much better (i.e., lower) values than the row on the left side of the room. The four light green values are clearly the outliers that were visible in Figure 4.3a. Using this information, it is possible to draw some conclusions about the effect of the position of the synthesized viewpoint relative to the objects in the scene, and select a few synthesized images that merit closer examination. The scene analysis visualization can also be used to visualize the *difference* between the error metrics ($\Delta L1$ and $\Delta SSIM$) of the regular and flow-based blending results, in order to show the improvement (or deterioration) of accuracy of the results when using flow-based blending compared to regular blending.

Sample Inspection In order to further understand the effects of the parameters on specific positions, some of the synthesized viewpoints from the scene analysis are examined by visually comparing the synthesized image to the ground truth image. The visual examination may also reveal information that the error metrics are unable to extract, such as specific types of artefacts. For example, by using the information presented in the scene analysis visualization in Figure 4.3b, it is possible to choose one of the best results, for example synthesized point K near the right wall in the middle. The close inspection of the synthesized images is shown in Figure 4.4: In the left column from top to bottom are the ground truth image, the regular blending result, and the flow-based blending result. In the right column are the L1 difference images to the ground truth image. They can help with understanding the error values. For example, the accuracy of the rug in the bottom face (marked in green) is improved in the flow-based blending result also has a fairly large artefact at the top of the door in the left face (marked in magenta), which is not the case in the regular blending result.



Figure 4.4.: Sample inspection of example viewpoint K. Depending on the content, different faces may be omitted.

4.3. Parameter Evaluation Using Virtual Scenes

In the first part of the evaluation, virtual scenes are used to evaluate the performance of the 2-DoF synthesis using regular blending and flow-based blending with different parameters. Virtual scenes allow full control over the external parameters, for example the scene geometry, and the positions of the captured and synthesized viewpoints, as well as enabling automatic generation of the images at the chosen positions. As a result, it is possible to test setups that would be unfeasible for real scenes, for example setups using a large number of captured viewpoints at varying locations in different scenes. The following three scenarios are tested using virtual scenes:

- "Different Scene Geometries" This scenario tests the effect of various scene geometries on the results. This includes the *basic shape* of the scene as well as the *objects within the scene*.
- "Density of Captured Viewpoints" This scenario tests the effect of the *density* of the captured viewpoints on the results. The density of the viewpoints is defined by how closely together the viewpoints are captured throughout the scene.
- "Position of Synthesized Viewpoints Relative to Captured Viewpoints" This scenario tests the effect of the *relative position* of a synthesized viewpoint *compared to the captured viewpoints*, for example how close a synthesized viewpoint is to a captured viewpoint.

The virtual scenes used in the scenarios are presented in Section 4.3.1, and the method of obtaining optical flow for these scenes is described in Section 4.3.2. Then, in Section 4.3.3, the setup of each scenario is described in detail, and the results of the evaluation of each scenario are presented and discussed. Finally, the insights from the evaluations of all of the scenarios are summarized and discussed in Section 4.3.4.

4.3.1. Data Acquisition and Featured Scenes

Three different virtual scenes are employed for the scenarios, modeled using the animation software Blender [Ble20]: the *checkersphere scene*, the *square room* and the *oblong room*.

Checkersphere Scene The *checkersphere scene* is a perfect sphere with a radius of approximately 2m. Its surface is covered with a checkerboard pattern with alternating colors of dark blue, dark red, and dark green. Although this kind of room is not likely to exist in reality, it represents an interesting case, since the scene geometry is identical to the proxy geometry. The checkerboard pattern is chosen so that distortions or inaccuracies are more visible. A latlong image from the center of the scene and a reference view from the outside of the checkersphere scene are shown in Figure 4.5.

Square Room The square room is a room whose basic shape is a perfect cube with a side length of 3.5m. It contains an assortment of furniture³: In one corner, there is an orange, L-shaped couch with dark blue and white cushions on it. In front of the couch is a small, white marble coffee table with a dark blue bowl on it. Several small, simple black and white pictures are hanging on the wall behind the couch. There is a blue and white rug in the middle of the room, and to the left of the couch are a round blue table, as well as a white



(a) Latlong image taken at the center of the sphere



(b) View from the outside for reference

Figure 4.5.: Overview of the "checkersphere scene"



(a) Latlong image taken at the center of the room



(b) Top view



Figure 4.6.: Overview of the "square room"

(a) Latlong image taken at the center of the room

(b) Top view

Figure 4.7.: Overview of the "oblong room"

radiator. On the wall next to the blue table is a white marble bookshelf containing several red books, as well as three wine bottles, and two decorational objects in green and purple. Across from the couch is a low marble TV cabinet carrying a black monitor, a black laptop and a black speaker. To the left of the cabinet is a wooden door with a gray handle. The walls are brick, painted a dark purple, and there is a lamp with a white lampshade hanging from the middle of the ceiling. Figure 4.6 shows an image taken in the center of the room as well as the top view.

The purpose of using the square room is to have a basic shape that is similar to the proxy sphere geometry, while at the same time offering a more realistic indoor setting.

Oblong room The *oblong room* has a room size of approximately 5.5m x 3.5m and contains the same basic elements as the square room. It has the exact same furniture layout as the square room, except that the basic shape of the room is different. The walls are dark blue, instead of dark purple, in order to be able to differentiate between the square and oblong rooms at a glance. An image taken in the center of the room, as well as the top view are shown in Figure 4.7.

Since the results of the different scenes are compared, it is necessary to choose comparable captured viewpoints, since these are used as input for the synthesis. Since the scenes all have similar scale, the viewpoint layout is chosen to be identical in all of the scenes: All scenes contain 36 captured viewpoints, aligned in a regular grid of 6x6 viewpoints, with 60cm spacing. The grid of viewpoints is centered within the scene. This means that in the checkersphere scene (Figure 4.8a) and the square room (Figure 4.8b), the viewpoints cover approximately the complete scene, and in the oblong room there is a 1m wide area on each side of the grid that is not covered (Figure 4.8c). It is necessary to take this difference in viewpoint coverage into account for the evaluation, since the viewpoints in the oblong room have a larger distance to two of the walls, which may have an effect on the accuracy of the results.

Since Blender is designed for creating animated movies, and not for capturing static viewpoints, some adjustments have to be made to be able to capture the chosen viewpoints as well as the ground truth images: After choosing the positions of the input viewpoints for the scenes, the position of the camera for each captured viewpoint is stored as a keyframe, so that the batch of viewpoints can be rendered like an animation. A Blender script is used in order to automatically assign the viewpoints and the ground truth points to the keyframes, and write out the metadata. This way the locations of the viewpoints are accurate, and the "capture" of the viewpoints requires no manual effort. The images are rendered with a resolution of 1000x500 for all of the scenes, in order to reduce the computation time for the image synthesis in the tests.

 $^{^{3}\}mathrm{The}$ https://www.cgtrader.com/free-3d-models/ adapted furniture models are from interior/living-room/low-poly-interior-57731178-c955-4625-9e44-109c8eea5ee2, by https://www.poliigon.com/ "miha29076", and textures adapted from user the are https://www.poliigon.com/texture/fabric-denim-003, texture/plaster-17, https:// www.poliigon.com/texture/wood-fine-dark-004, and https://www.poliigon.com/texture/ interior-design-rug-starry-night-001. All accessed last on September 23, 2020





(a) The captured viewpoints in the checkersphere scene

(b) The captured viewpoints in the square room



(c) The captured viewpoints in the oblong room

Figure 4.8.: The grid of captured viewpoints in each scene, including the proxy geometry as a gray circle. The scene sizes are not to scale.

4.3.2. Synthesizing Optical Flow with Blender

Using Blender to create virtual scenes not only facilitates capture, but also offers an alternative to calculating optical flow. As mentioned in Section 2.1.2, most optical flow algorithms struggle with large displacements. The flow-based blending step in the 2-DoF synthesis algorithm, on the other hand, assumes acceptably accurate optical flow and there is no attempt to judge whether the optical flow calculation is feasible between two selected viewpoints. As a result, given the wrong circumstances (two input viewpoints **A** and **B** that are far apart), the optical flow algorithm may fail, leading the flow-based blending to output undesirable results. The success of the optical flow algorithm is a prerequisite for the success of the 2-DoF algorithm with flow-based blending.

Contrarily, the focus of this evaluation is not the accuracy of an arbitrary optical flow algorithm. In the best case, it would be possible to emulate "perfect" optical flow, thus decoupling the success of the optical flow from the success of the flow-based blending. While this is practically impossible for real scenes, virtual scenes theoretically contain all necessary information for retrieving "ground truth" optical flow. Blender, for example, is capable of "rendering" motion vectors using its vector speed render pass, which calculates the movement between points from one frame to the next in pixel space. The result is a motion vector field, which corresponds to the result of a "classic" optical flow algorithm. This "ground truth" optical flow (in the optimal case) was first presented by Butler et al. [BWSB12] as a benchmark for optical flow algorithms.

In order to demonstrate the improvement of Blender optical flow compared to Farnebäck optical flow, which is the optical flow algorithm in the implementation used for this evaluation, a small scene setup is tested using 1-DoF interpolation. Figure 4.9a shows the test setup: 25 viewpoints are interpolated at the interpolation distance $\delta = 0.5$ between captured points. Each of the 25 viewpoints is interpolated twice: Once using Farnebäck optical flow, and once using Blender optical flow. The results of both interpolations are then compared using the error metrics. Figure 4.9b shows the improvement of the results using Blender optical flow: In all but one case for the L1 values, and in the majority of the SSIM values, the Blender optical flow improves the error values, shown by the positive values in Figure 4.9b. Visually, the improvement by using Blender optical flow is clear: Figure 4.9c shows the viewpoint I interpolated using Farnebäck optical flow, and Figure 4.9d the same viewpoint using Blender optical flow. There are distincly fewer artefacts with Blender optical flow, for example the rug and the couch both have a much more distinct outline, and the bookshelf is also clearer. Figure 4.9e and Figure 4.9f show the same for interpolated viewpoint M. In this case, the TV cabinet and the rug are much clearer in the Blender optical flow version (Figure 4.9f).

It is notable that using Blender optical flow tends to improve the results compared to Farnebäck's algorithm, but that does not mean that the resulting optical flow is completely accurate. For example, the bookshelf in the right and middle faces in Figure 4.9d still shows warping and doubling effects, indicating that there are still some inaccuracies. The same is true for the coffee table and the blue round table in the bottom face. There are several possible reasons for this, mostly based on the fact that the process in Blender, like most optical flow algorithms, is designed for frame-to-frame use, and has in this case been "misused" for movements between frames that are unrealistic for an actual animation. Nevertheless, no definitive explanation can be made at this point, since this would require in-depth understanding of Blender's vector speed render pass, which is outside of the scope



(a) The interpolated viewpoints A-Y (in orange) for testing optical flow



(c) 1-DoF interpolated viewpoint I using Farnebäck optical flow



(e) 1-DoF interpolated viewpoint M using Farnebäck optical flow



(b) The improvement of error values using Blender optical flow vs Farnebäck optical flow. Here, a positive value signifies a reduction of the error value.



(d) 1-DoF interpolated viewpoint I using Blender optical flow



- (f) 1-DoF interpolated viewpoint M using Blender optical flow
- Figure 4.9.: Comparing 1-DoF interpolation results using Farnebäck to results using Blender optical flow

of this thesis. Based on the results shown in Figure 4.9, and experience gained from testing both variants, the Blender optical flow is used for the tests, because, even though it is not completely accurate, it still seems to mostly yield better results than Farnebäck's optical flow algorithm and as such decouples to a degree the success of the synthesis with flow-based blending from the success of the optical flow algorithm.

4.3.3. Scenarios and Results

Using the generated scenes and optical flow, it is now possible to test and evaluate the scenarios "Different Scene Geometries", "Density of Captured Viewpoints" and "Position of Synthesized Viewpoints Relative to Captured Viewpoints". For each scenario, the scenes, viewpoint setups, and tested parameters are presented. Then, the *regular blending results* (i.e., the results of the synthesis using regular blending) are discussed, followed by the *flow-based blending results* (i.e., the results of the synthesis using flow-based blending results in order to determine the impact of the synthesis using flow-based blending on the performance compared to the synthesis using regular blending on the performance compared to the synthesis using regular blending on the synthesis of the scenario evaluation are summarized.

Scenario 1: Different Scene Geometries

The first parameter to be examined is the effect of different scene geometries on the accuracy of the results. There are two different attributes of scene geometry that may have an influence on the result: the basic shape of the scene (e.g., sphere, cube, rectangular prism, or arbitrary polygon), and the objects within the scene. Both of these attributes are considered in the evaluation. All the scenes presented in Section 4.3.1 are used for testing, as they differ both in their basic shape, as well as in the arrangement of the objects within, although the square room and the oblong room are more similar to each other than to the checkersphere scene.

The arrangement of captured viewpoints in all the scenes is identical (a 6x6 grid with a spacing of 60cm), and 25 viewpoints are synthesized in each scene, shown in Figure 4.10: The synthesized points are near the center or in the center of each grid cell, since these are the areas where the deviation angles are the highest, and where the largest artefacts for the regular blending are expected to emerge. In the square and oblong rooms, the synthesized points are slightly offset from the center of each grid cell. This offset is necessary in order to test actual 2-DoF synthesis, instead of just 1-DoF interpolation, since synthesizing a viewpoint in the center of a grid cell could be done with only 1-DoF interpolation (e.g., by interpolating by 0.5 between the top right and the bottom left captured viewpoint, as done in Section 4.3.2 for testing Blender optical flow). No offset is used in the checkersphere scene, since the checkersphere scene is expected to have excellent results for the regular blending (since the proxy geometry and scene geometry are identical). In this case it is more interesting to use one of the presumably best positions for the flow-based blending to see how well it holds up in comparison.

Regular Blending Results The boxplot in Figure 4.11a shows the distributions of the error values for the regular blending results in the three scenes. The most striking feature of this distribution is that the checkersphere scene results show the highest error values for the L1 error, whereas they show the lowest values for the SSIM error. At first, this seems





(c) The oblong room

Figure 4.10.: The captured (blue) and synthesized (orange) viewpoints in the different scenes (scenes are not to scale)



Figure 4.11.: Comparing the distributions of the results in different scenes



Figure 4.12.: Results for synthesized viewpoint Y in the checkersphere scene: The regular blending result is very close to the ground truth, except for some blurriness. The flow-based blending result shows some inaccuracies (magenta) and noise (green)

surprising, both because the error metrics do not "agree", as well as because the results of the regular blending are expected to be very accurate since the scene geometry is identical to the proxy geometry. The reason for the comparatively high L1 values is the sensitivity of the L1 metric to different color values. L1 errors on the images of the checkersphere scene will generally produce a higher value than in other scenes because of the checkerboard texture: The difference between a dark blue pixel of a dark checkerboard field, and a white pixel on a white checkerboard field is close to 1, whereas the difference between a dark brown pixel and a dark purple pixel (e.g., between the door and the wall in one of the rooms) will produce a lower error value, although the distortion or displacement may be identical. The SSIM error metric, which does not take the color values of the pixels into account, produces a distribution that is much closer to the expected result: Since the scene geometry is identical to the proxy geometry, the result of the reprojection should be almost perfect. And in fact, when visually comparing the results of a synthesized viewpoint to the ground truth (the first two rows in Figure 4.12), the only difference is a little bit of blurriness due to sampling differences. The white lines in the L1 difference depicted in the right column of Figure 4.12 show how the blurriness causes the high L1 error.

The trend of the error metrics of the other two rooms is consistent: Both the L1 and SSIM error values of the square room are generally higher than those of the oblong room. In



(a) Error values of regular blending in the square room



(b) Error values of regular blending in the oblong room

Figure 4.13.: Scene analysis visualization of regular blending results in the square and oblong rooms. Higher values indicate "worse" accuracy and lower values indicate "better" accuracy.

this case, comparing the RGB color values is more reliable, since both rooms use the same textures. The results however, are surprising: Although the basic geometry of the square room is closer to the proxy geometry, the error values in the square room are generally higher than those in the oblong room. A closer scene analysis shows the likely reason for this: The scene analysis visualization of the square room in Figure 4.13a shows that the error values are particularly high near the bookshelf on the left side of the room, whereas in the oblong room in Figure 4.13b the bookshelf is farther away from the viewpoints and the values on the left side of the room are very low. The inspection of the synthesized images at location O (closest to the bookshelf), shown in Figure 4.14, confirms this presumption: The bookshelf is so close to viewpoint O in the square room, that there are extreme inaccuracies in the synthesis due to large deviation angles. In the oblong room, the bookshelf is much farther away, making the devation angles much smaller and the result more accurate. The larger net distance to the walls and some of the objects in the oblong room is the likely reason for the lower error values throughout the scene.

As for the accuracy of the synthesized viewpoints relative to other objects in the square room, Figure 4.13a shows moderately high error values in the second row from the bookshelf (D, I, N, S, X), and in the top row (E, D, C, B, A) and the bottom row (Y, X, W, V, U), and lowest in the center and right side of the room (H, G, F, M, L, K, R, Q, P). This is likely due to the proximity of the viewpoints to the walls, and the objects in the scene. The closer a viewpoint is to the walls (i.e., the edge of the scene), the higher the deviation angles are, and thus, the ghosting artefacts and positional inaccuracies. The bookshelf is especially close to the viewpoints, since it is at eye-level, instead of below (and thus farther away, with smaller deviation angles), like the majority of other objects. The same effects are visible in the oblong room in Figure 4.13b, although the synthesized viewpoints are generally farther away from objects, due to the shape of the scene. Near the top wall (E, D, C, B, A), the error values are generally higher, and especially so over the blue table (D) and over the sofa (A). In the bottom row, the viewpoints near the TV cabinet (U, V) are also higher than in the rest of the scene, whereas the bottom left viewponts (O, N, T, S, Y, X) are the lowest in the scene, and also relatively far away from any objects.

Flow-based Blending Results The boxplot in Figure 4.11b, which shows the distribution of error values of the flow-based blending results in the three scenes, displays similar tendencies as the error values of the regular blending results: The L1 values of the checkersphere scene are very high, and the results of the oblong room generally have lower values than those of the square room. One exception is the SSIM error value of the checkersphere scene: Whereas the SSIM error in the checkersphere scene is significantly lower than the other two for the regular blending results, in the flow-based blending results, the SSIM error yields worse results than the oblong room, but still mostly better than the square room. The worse performance of the flow-based blending in the checkersphere scene is likely due to inaccuracies introduced by the flow-based blending, for example imperfect optical flow, or ray approximation. The last row in Figure 4.12, which displays the flow-based blending result, shows larger inaccuracies than the regular blending result as well as some artefacts and noise, which are the probable causes for the higher error values.

In the other cases, the flow-based blending results mirror those of the regular blending: The error values in the oblong room are generally lower than those in the square room. A look at the scene visualization in Figure 4.15 shows that the flow-based blending results



Figure 4.14.: Regular blending result of viewpoint O in the square and oblong rooms: The bookshelf has a strong impact on the difference in error values (marked in green)





(a) Error values of flow-based blending in the square room

(b) Error values of flow-based blending in the oblong room

Figure 4.15.: Scene analysis visualization of flow-based blending results in the square and oblong rooms

display very similar tendencies as the regular blending results: Like in the regular blending case, the reason for the worse performance of the square room is very likely also the relative position of the walls and objects to the synthesized viewpoints. The most severe case is the area around the bookshelf. In the case of the regular blending, this area is problematic due to the large deviation angles leading to inaccurate reprojections. Generally, the flow-based blending should alleviate this problem, however, in this case it does not (or not considerably). The reason for this is that the optical flow calculation fails in proximity to the bookshelf, which is shown in Section 4.3.2. As a result, the normally straight lines of the books are warped, but a comparison to the ground truth shows that they are warped in a way that bears no resemblance to the actual position or shape (for details, see Figure A.2 on page 95).

The general relation of the accuracy of the results to the proximity of the objects in the scene is very similar to the observations of the regular blending results: Viewpoints that are closer to objects or walls tend to have higher error values (e.g., W, V, U in the square room and D, A, and U in the oblong room) while viewpoints that are farther away from objects have lower error values (L, K in the square room, O, N, T, S in the oblong room). These tendencies are much more pronounced in the oblong room, where the differences in distance are higher.



Figure 4.16.: Comparing the distribution of the results in different scenes for regular blending and flow-based blending

Comparing Regular Blending to Flow-based Blending Results The boxplot in Figure 4.16 displays the distributions of the error values of both the regular blending (purple) and the flow-based blending (blue), as well as the error value distribution of the naïve algorithm (orange) for comparison⁴. The graph shows that the error values of the results of the flow-based blending are generally slightly better (i.e., lower) than those of the regular blending (except in the case of the checkersphere scene) and that the error values of the results of the regular blending tend to be distinctly better than those of the naïve algorithm.

In the case of the checkersphere scene, where the scene geometry is identical to the proxy geometry, the regular blending distinctly outperforms the flow-based blending. However, this is to be expected. The goal of the flow-based blending approach is to improve problems that arise due to the difference between the real and proxy geometries, and it introduces possible inaccuracies in order to do so (e.g., viewpoint selection, optical flow, ray approximation). Therefore, it is not surprising that the results are less accurate than the results of the regular blending when the proxy geometry is identical to the actual geometry.

For the square room and the oblong room, the $\Delta L1$ and $\Delta SSIM$ (i.e., the difference, or "improvement") of the flow-based blending compared to the regular blending are shown in Figure 4.17. Positive $\Delta L1$ and $\Delta SSIM$ values (red) signify that the flow-based blending produced a *worse* result (i.e., higher error value) than the regular blending, and negative $\Delta L1$ and $\Delta SSIM$ (blue) signify that the flow-based blending produced a *better* result (i.e., lower error value) than the regular blending, with stars marking the highest and lowest values. At a glance, it is clear that in all cases in the oblong room, and in all but one or two

⁴The naïve algorithm error values of the checkersphere scene are omitted because they are so much higher than the other values that the scale of the plot would be too small.



Figure 4.17.: $\Delta L1$ and $\Delta SSIM$, "improvement" of flow-based blending over regular blending results in the square and oblong rooms. The stars denote the best and worst cases.



Figure 4.18.: Synthesized point A in the oblong room (best improvement): The flow-based blending drastically improves ghosting artefacts on the couch. See Figure A.3 (page 96) for more details.

cases in the square room (depending on the metric) the flow-based blending improves the result based on the L1 and SSIM error metrics.

The "best improved" result with the lowest $\Delta L1$ difference in the oblong room is viewpoint A, which is in the top right corner of the scene (marked with a star in Figure 4.17). Figure 4.18 shows the left face of viewpoint A. Here, the most visible difference is the couch: Where the inner edge of the couch shows severe ghosting artefacts in the regular blending result, it is much cleaner in the flow-based blending result (marked in magenta). More details of this result can be seen in Figure A.3 on page 96.

The "worst improved" viewpoint L near the middle of the scene shows that the flow-based blending result also introduces new artefacts: The rug in the bottom face of the flow-based blending result, shown in Figure 4.19, has a few extreme discontinuities, where the shape of the rug seems fragmented with sharp edges. The rest of the image also shows some of these discontinuities; however, most objects are positioned more accurately, which can be seen in more detail in Figure A.4 on page 97. These severe discontinuities are caused by the selection of input viewpoints for flow-based blending: For each ray of the synthesized image, two input viewpoints are selected based on their deviation angle, and whether they are "on either side" of the ray in question (see Section 3.1.3). This means that while traversing the rays of a synthesized viewpoint, there comes a point where the selected captured viewpoints for the 1-DoF interpolation **A** and **B** suddenly switch to **B** and C^5 , for example. This will be described in more detail in Section 4.3.4. In these cases, the less accurate the reprojection step is, the more extreme the discontinuity at that place in the image seems to be. Although these discontinuities are visually extremely irritating, it is possible that they do not have a large impact on the error metrics.

As for the square room, the "best improved" result with the lowest $\Delta L1$ difference in the square room is viewpoint N. Figure 4.20 shows the results of the bottom face of this viewpoint. The most visible difference is the rug (marked in magenta): In the regular blending result, it shows some ghosting (doubled, offset edges), which has been mostly fixed

⁵In this case, viewpoints **A**, **B** and **C** denote captured input viewpoints as in Chapter 3 and not synthesized viewpoints.



Figure 4.19.: Synthesized point L in the oblong room (worst improvement): The flow-based blending result introduces some severe discontinuity artefacts on the rug. See Figure A.4 (page 97) for more details.

in the flow-blending result. Other than that, the white coffee table is slightly blurrier, but covers a more accurate area than the regular blending blending result (marked in cyan). The bottom part of the bookshelf is also more accurate (marked in green). Otherwise the two results are very similar visually, shown in Figure A.5 on page 98.

For the "worst improved" viewpoint L, which is near the center of the scene, the regular and flow results are also visually very similar. Like for viewpoint N (Figure 4.20, some of the ghosting artefacts in the regular blending result are gone in the flow-based result. However, the flow-based blending also introduces some discontinuity artefacts, like in viewpoint L in the oblong room (Figure 4.19. These discontinuities could be the reason for the higher error value (for details see Figure A.6 on page 99).

Scenario Synopsis The goal of this scenario is to evaluate the effects of the scene geometry on the accuracy of the results of regular and flow-based blending. This includes the details of the geometry given by the shape and placement of objects within the scene, as well as the general shape of the scene. Concerning the geometry details, i.e., the objects within the scene, the results of the scenario are fairly clear: both blending techniques perform better, the more distance the synthesized point has from specific objects. The closer the synthesized point is to an object, the more ghosting and doubling artefacts, and positional inaccuracies show up in the regular blending results. In most of these cases, the flow-based blending synthesizes a more accurate image, showing fewer positional inaccuracies and correctly synthesizing some of the object shapes. However, the flow-based blending also introduces some new artefacts, predominantly abrupt discontinuities. These discontinuities are not necessarily recognized by the error metrics and need to be identified by visual inspection. In the case of extreme proximity to an object (e.g., in front of the bookshelf), both the regular blending and the flow-based blending produce highly inaccurate results. In the case of the flow-based blending, this is likely due to inaccurate optical flow. However, even in the cases where the optical flow is inaccurate, the flow-based blending result is not worse (in terms of the error metrics) than the regular blending result.


Figure 4.20.: Synthesized point N in the square room (best improvement for L1, good for SSIM): The flow-based blending removes the ghosting artefacts on the rug (magenta) and improves the accuracy on the coffee table (cyan), and the lower part of the bookshelf (green). See Figure A.5 (page 98) for more details.

As for the impact of the general shape, the results are not very significant, due to the choice of the oblong and square rooms along with the chosen captured and synthesized viewpoints. The large distance of the objects and walls to the synthesized viewpoints in the center of the scene in the oblong room overpowers most effects that the different basic shape might have. It is clear, however, that in the case where the scene geometry matches the proxy geometry in the checkersphere scene, the flow-based blending performs worse than the regular blending.

Scenario 2: Density of the Captured Viewpoints

The previous scenario demonstrated that close proximity of a synthesized viewpoint to an object can have a strong adverse effect on the accuracy of the result. A possible way to mitigate this problem could be to increase the density of the captured viewpoints near objects and walls. The scenario presented in this section explores the impact of viewpoint density on the accuracy of the results.

To test the effect of viewpoint density, the square room is used, since the viewpoint grid covers the entire area of the room, which guarantees higher proximity to all of the objects. Three different versions of the grid of captured viewpoints are used: a 2x2 grid with a spacing of approximately 2.3m (Figure 4.21a), the 6x6 grid with a spacing of approximately 60cm, which was also used in the previous scenario (Figure 4.21b), and a 12x12 grid with a spacing of approximately 30cm (Figure 4.21c). The 2x2 grid is chosen since it is the minimal grid to cover the entire room, and the 12x12 grid is chosen, since it halves the distance of the 6x6 grid and as such, retains the relative position of the captured viewpoints compared to the synthesized viewpoints. If a different grid was used, for example 10x10, some synthesized viewpoints would be closer to captured viewpoints than other synthesized viewpoints, which may have an effect on the overall results. As in the previous scenario, 25 viewpoints are synthesized, located near the center of each grid cell. They are offset slightly from the exact center, like in the previous scenario, to demonstrate true 2-DoF synthesis.



Figure 4.21.: The different captured viewpoint densities (blue) in the square room with the synthesized viewpoints (orange)



Figure 4.22.: Comparing the distributions of the results in the square room with different densities separately



(a) Results of regular blending (b) Results of regular blending (c) Results of regular blending with a 2x2 grid with a 6x6 grid with a 12x12 grid

Figure 4.23.: Scene analysis visualization of the regular blending results in the square room with different densities

Regular Blending Results The boxplot in Figure 4.22a shows the general distribution of the results of the regular blending with varying viewpoint densities. Unsurprisingly, the accuracy of the results improves, the higher the density of the input viewpoints is. In the 6x6 and the 12x12 setup, there are several outliers with a higher error value for the L1 error, which are likely due to the proximity of some points to the bookshelf. In the 2x2 setup, there are no significant outliers, which means that the distribution of the error values is more uniform throughout the scene.

A look at the scene analysis visualization in Figure 4.23 confirms these assumptions: The outliers in the 6x6 (Figure 4.23b) and 12x12 (Figure 4.23c) setups are caused by the bookshelf on the left side of the room. In the case of the 2x2 setup (Figure 4.23a), the error values are fairly high throughout, compared to the other two setups, which is the reason that the viewpoints near the bookshelf do not register as outliers. Other than the area around the bookshelf, both the 6x6 and the 12x12 scenes have a fairly uniform distribution for the L1 error. For the SSIM error, the areas close to the walls have a slightly higher error than those in the middle of the scene. This is in line with the results of the previous scenario, where the error values near objects or walls tended to be higher.

In order to understand more about how the density affects ghosting and other artefacts in the images, one of the better and one of the worse results for all of the setups is examined visually. According to the general tendencies of the values in the different setups, synthesized viewpoint T near the bottom left of the room, next to the bookshelf has a comparatively high error value in both metrics for all three scenes and synthesized viewpoint G, above the coffee table towards the top right corner has a comparatively low error value for all of the

scenes.

Figure 4.24 shows the bottom face of the regular blending results of viewpoint T which displays the most prominent reason for the high error values: for the 2x2 scene, while most of the scene is moderately accurate (the objects are in approximately the right place), the bookshelf is shown from the wrong perspective, i.e., from the side versus from the front (marked in magenta). The reason for this is that the viewpoint used for reprojection captured the bookshelf from the side. Using only this information, it is impossible to reconstruct the front of the bookshelf. One other effect of the fairly large change in perspective when using regular blending are the warped walls (marked in cyan). This effect is caused by the use of a sphere as proxy geometry, which has curved "walls". The warping problems are much less visible in the 6x6 and 12x12 results, since the distance between the captured and synthesized viewpoints is much smaller, which leads to less distortion. The L1 difference images on the right do show an improvement of the accuracy in the 12x12 image over the 6x6 image, but the bookshelf still has many inaccuracies due to its proximity and high detail. More details of this viewpoint are shown in Figure A.7 on page 100.

The difference between the 12x12 and the 6x6 image is less evident in G, one of the worse results. Figure 4.25, which shows the bottom face of viewpoint G, clearly illustrates the effect of the denser grid. The 2x2 image is an excellent demostration of the problem with using input images with large deviation angles in conjunction with a proxy geometry that is not identical to the scene geometry: The rays used to synthesize this image captured the coffee table at different positions and the reprojection does not account for this, since it only approximates the scene geometry. As a result, the coffee table appears four times in different locations. In Figure 4.25, the reprojection errors decrease visibly as the density increases: in the 6x6 image, a slight doubling effect of the coffee table is still visible, whereas in the 12x12 image, the table only appears slightly blurry. The effects on the rest of the faces (shown in Figure A.8 on page 101) are less distinct, since the distance to the objects is larger in the rest of the image.

Altogether, the error values near objects and walls are slightly higher in both the 6x6 and 12x12 setups, but the improvement when going from the 6x6 to the 12x12 density is also higher in these areas. This can be seen in Figure 4.26a, which shows the improvement when using the 12x12 scene versus the 6x6 scene with regular blending. In areas near walls (e.g., the top row for both metrics, viewpoints A-E), or objects (in front of the bookshelf for L1 (O, T), or in front of the TV screen for L1 and SSIM (U,V,W)), the improvement tends to be higher than near the center of the scene (e.g., viewpoints H, G, M, L). This means that a higher density has a larger impact on the accuracy near objects and walls than on viewpoints that are farther away.

Flow-based Blending Results The error values of the flow-based blending results in the boxplot in Figure 4.22 show similar tendencies as the regular blending results. Like for the regular blending, the 6x6 and 12x12 setups have several outliers in the L1 metric, but otherwise a fairly close distribution. The scene analysis visualization in Figure 4.27 also shows a similar pattern: In the 2x2 scene, the error values are generally high, whereas in the 6x6 and 12x12 scenes, the error values are high near the bookshelf, but generally similar everywhere else. Like in the regular blending scene, the improvement of the values in the 12x12 setup compared to the 6x6 setup is slightly higher near the walls, shown in Figure 4.26.



Figure 4.24.: The bottom faces of the regular blending results for point T (one of the worse results) with different densities: The 2x2 image shows the bookshelf from the wrong perspective (magenta), and the walls are noticeably warped (cyan), which is improved in the 6x6 and 12x12 images. See Figure A.7 (page 100) for more details.



Figure 4.25.: The bottom faces of the regular blending results for point G (one of the better results) with different densities: Both the accuracy and the ghosting effects are visibly reduced, the higher the density of the captured viewpoints is, which is especially clear for the coffee table. See Figure A.8 (page 101) for more details.



(a) Improvement for regular blending

(b) Improvement for flow-based blending

Figure 4.26.: Improvement of results using 12x12 density compared to 6x6 density



ing with a 2x2 grid ing with a 6x6 grid ing with Figure 4.27 : Scene analysis visualization of the flow based blending r

ing with a 12x12 grid

Figure 4.27.: Scene analysis visualization of the flow-based blending results in the square room with different densities



Figure 4.28.: Distributions of error values in the square room with different densities of captured viewpoints for the regular blending and flow-based blending

Comparing Regular Blending to Flow-based Blending Results Looking at the boxplot in Figure 4.28, it is clear that both the regular blending and the flow-based blending perform distinctly better than the naïve algorithm. Other than that, the distributions of the regular blending and flow-based blending results are inconclusive. For the 2x2 scene, the median L1 error is slightly higher for the flow-based blending, while the error range is lower. The SSIM error range and median for the 2x2 scene are both lower for the flow-based blending. In the 12x12 scene, the L1 error shows an almost identical distribution, whereas for the SSIM result, the general distribution of the flow-based blending is wider (ignoring outliers), which implies that some results were improved while others were worsened. Only the results of the 6x6 scene show a consistent improvement of the flow-based results compared to the regular results for both error metrics.

To investigate the inconclusive results of the 2x2 and 12x12 setups, a closer look at the scene analysis visualization is required. Figure 4.29 shows the $\Delta L1$ and $\Delta SSIM$ of the flowbased blending versus the regular blending for the 2x2 and the 12x12 scenes. The reason for the inconclusive L1 error distribution of the 2x2 setup (improved range but worse median) is more clear in the scene analysis visualization: The majority of results are improved, especially near the walls, however, there are also some results that have distinctly higher error values (e.g., L and K). This accounts for the higher median error value. The 12x12 setup also shows clearly improved values of the flow-based results nearer to the walls, and a slightly worse values near the center of the room.

For the 2x2 scene, the regular blending produces relatively inaccurate results, due to the extreme perspective changes. The flow-based blending relies on optical flow, which does not handle large displacements well. The results show that in the $2x^2$ scene, the optical flow algorithm does not produce very accurate results in general, either, which is visible in both the "best" and "worst improved" images. The "best improved" viewpoint T, shown in Figure 4.30, is one of the worst rated results of the regular blending, since it does not show the bookshelf from the correct perspective. In the flow-based version, a blurry shadow of the bookshelf is visible; however, the whole image contains blurry distortions of all of the objects. So although the metrics show improved values, visually it is much harder to distinguish the different objects. More details are shown in Figure A.9 on page 102. The same holds true for the "worst improved" viewpoint K on the right side of the scene in the center, where both metrics measure a slight increase in error value from the regular to the flow-based result. For this viewpoint, the regular blending result shows extreme doubling artefacts, and the flow-based version, due to the failure of optical flow, exacerbates the problem: almost all of the objects blurred to the point where they are hardly recognizable, like in the previous "best improved" viewpoint. The resulting images are shown in Figure A.10 on page 103. In summary, it is clear that the captured viewpoints in the 2x2 density are too far apart to produce satisfying results with either blending technique.

As for the 12x12 scene, the error metrics in Figure 4.29b show a slight decrease in error values near the walls, and a slight increase of error values near the middle of the scene. However, when looking at the best and worst improved viewpoints (Y and H, respectively), very little difference is actually visible. In the "best improved" viewpoint Y in the bottom left corner of the scene, the flow-based blending slightly improves the accuracy of several objects, although some ghosting artefacts remain. However, other than that, the two images are visually extremely similar, shown in Figure A.11 on page 104.

The same holds true for the "worst improved" viewpoint H near the center of the room, the bottom face of which is shown in Figure 4.31: Looking at the L1 difference images, it is



Figure 4.29.: $\Delta L1$ and $\Delta SSIM$, "improvement" of flow-based blending over regular blending results in the 2x2 and 12x12 setups. The stars denote the best and worst cases.



Figure 4.30.: Bottom face of synthesized point T in the 2x2 setup (best improvement for L1, good for SSIM): The flow-based blending synthesizes a blurry approximation of the bookshelf, but also distorted and blurred the rest of the image.



Figure 4.31.: Bottom face of synthesized point H (worst "improvement": slight increase of error): The flow-based blending result synthesizes the coffee table and white pillow with cleaner edges (magenta), however, due to a bug in an external library, the flow-based blending result contains some black lines (green).

hard to see any difference between the two, but when comparing the synthesized images, it is noticeable that the flow-based blending produces cleaner outlines on the coffee table and the white pillow than the regular blending, where there are some ghosting artefacts (marked in magenta). This change hardly has an effect on the accuracy however, and possibly does not have a noticeable impact on the error values. The rest of the faces, shown in Figure A.12 on page 105, are extremely similar. A factor that is possibly detrimental to the error value of the flow-based blending result are the black lines that appear near the face edges and are not present in the regular blending result (marked in green in Figure 4.31). These black lines originate from a bug in one of the external libraries and only affect the flow-based blending (explained in more detail in Section 4.3.4). In cases where the synthesized images are very similar, it is possible that these artefacts skew the results in favor of the regular blending.

The 6x6 setup is more straightforward than the 2x2 and 12x12 setups. The scene analysis visualization in Figure 4.32 shows the improvement of the flow-based blending results over the regular blending results, which is very similar to the improvement in the previous scenario for the square room (Figure 4.17a). Since these setups and results are very similar, the 6x6 setup is not examined in more detail.

Scenario Synopsis In summary it can be said that for the tested room (and presumably in most other cases as well), increasing the density of the captured viewpoints also increases the accuracy of the results. In the tested cases, the improvement is more apparent near objects and walls. As a result, it is most likely best to capture an irregular grid of viewpoints, with a denser distribution of captured viewpoints near objects and walls, and a sparser distribution where there are no objects.

In the extreme case of the 2x2 density, both the regular and the flow-based blending lead to extreme artefacts, due to the large jumps in reprojection and the failure of the optical flow algorithm. For the 6x6 density, the results are unambiguous: both metrics produce lower error values for the vast majority of flow-based blending results. The 12x12 density leads to



Figure 4.32.: $\Delta L1$ and $\Delta SSIM$, "improvement" of flow-based blending results over regular blending results in the 6x6 setup

comparatively low error values and few artefacts for both regular and flow-based blending. In this case, the metrics are ambiguous, since the difference between the two versions is very small. A visual evaluation of some of the samples indicates that the flow-based blending improves ghosting artefacts, which visually improve the images, but also introduces artefacts due to a bug in an external library, which may skew the results unfavorably.

Scenario 3: Position of Synthesized Viewpoints Relative to Captured Viewpoints

In most of the previous results, the flow-based blending showed an improvement over the regular blending. However, in the first two scenarios the locations of the synthesized view-points are chosen explicitly so that the regular blending would most likely have the most difficulty: areas near the center of the grid cells where the deviation angles are relatively high. Naturally, this is not the only location that comes in question for synthesis. In fact, all locations within the convex hull can potentially be synthesized by the 2-DoF algorithm. In order to gain a more general understanding of the impact of the relative positons of the captured viewpoints on regular versus flow-based blending, this scenario uses a dense grid of synthesized viewpoints, instead of choosing a few select locations in the scene.

Based on the insights gained from the last two scenarios, the square room is used with a captured viewpoint density of 6x6. The square room gives the advantage of covering the whole possible space, and a density of 6x6 with a spacing of 60cm is a conceivable distance for extrapolation to real scenes. A grid of 25x25 viewpoints is synthesized, totaling 625 synthesized points, shown in Figure 4.33.

Regular Blending Results In this scenario, only the position of the viewpoints within a single scene is examined, so the distribution can be inspected directly in the scene analysis visualization in Figure 4.34a. The dense coverage of synthesized viewpoints gives a fairly detailed picture of the effects of the location relative to the scene, and especially relative to the location of the captured viewpoints. It is immediately striking that the synthesized viewpoints in the close vicinity of a captured viewpoint have a distinctly lower error value than viewpoints that are farther away. The exceptions to this are the synthesized viewpoints near the walls and near the bookshelf. The observation of higher error values near the bookshelf and walls are consistent with the observations in the previous scenarios. However, this scenario shows that the error values are higher near walls and objects, independent



Figure 4.33.: The dense grid of synthesized viewpoints (orange) and the 6x6 grid of captured viewpoints (blue) in the square room



(a) Results of regular blending (b) Results of flow-based blending

Figure 4.34.: Scene analysis visualization of regular and flow-based blending results

of whether the synthesized viewpoints are close to the captured viewpoints or not. This phenomenon is clearly visible in the L1 error visualization, but even more so in the SSIM error visualization, where the accuracy dropoff is even more extreme.

Flow-based Blending Results The error values of the flow-based blending results (Figure 4.34b) display a different pattern than those of the regular results: While the error values are lower in the vicinity of captured viewpoints, they are comparably low in the vertical and horizontal spaces between the captured viewpoints, as well. This implies that it does not have a significant impact on the error values, whether a synthesized viewpoint is very close to a captured viewpoint, or anywhere between a set of horizontally or vertically adjacent viewpoints. In general, the majority of the values is fairly similar, with clear outliers only visible near the bookshelf.

Comparing Regular Blending to Flow-based Blending Results The scene analysis visualization in Figure 4.35 shows the $\Delta L1$ and $\Delta SSIM$ error values of the results of the flow-based blending compared to the results of the regular blending. Here, the results are striking: In



Figure 4.35.: $\Delta L1$ and $\Delta SSIM$, "improvement" of flow-based blending results over regular blending results for 625 synthesized images in the square room. The annotated points are examined more closely in the text.



Figure 4.36.: Bottom face of synthesized point 7: The accuracy of the pictures on the wall is better in the flow-based blending result (magenta), and the position of the coffee table is also more accurate (green). However, the black line artefacts (cyan) are also fairly severe. For more details see Figure A.13 on page 106.

general, the error values of synthesized points in close proximity to captured points increase (i.e., the accuracy decreases) when using flow-based blending. An exception to this are the areas near the walls of the room: In these cases, the flow-based blending improves the results in the majority of cases. Also, in the areas where the distance to the captured viewpoints is highest (i.e., near the center of a grid cell), the flow-based blending also performs better. An area where the results are ambiguous is the area near the bookshelf. Here, the improvement or degradation cannot be clearly attributed to the proximity to a captured viewpoint or the proximity of the bookshelf. It must be kept in mind, however, that in the case of the bookshelf, the Blender optical flow does not yield good, or even acceptable results, which has a direct, detrimental effect on the flow-based blending, so the results near the bookshelf should not be taken into strong consideration.

Many cases where the flow-based blending yields a better result than the regular blending have already been shown in the previous scenarios. In this scenario, it is more interesting to examine the cases in which the flow-based blending performs only slightly better, or worse than the regular blending, in order to understand possible problems caused by the flow-based blending algorithm.

Starting with an example where the flow-based blending performs slightly better than the regular blending, Figure 4.36 shows the bottom face of viewpoint 7, which is at the top edge of the room. Although the error value is not significantly lower than that of the regular result, the accuracy is visibly improved, as well as there being no discontinuities or doubled edges. This is especially visible on the coffee table (marked in green), and the pictures on the wall (marked in magenta). A possible reason for the comparatively small improvement of the error values despite the visually clear improvement could be the black line artefacts that are caused by the external library bug (marked in cyan). Similar details are also visible in the rest of the faces, shown in Figure A.13 on page 106.

Next, a result near the middle of the scene is examined (Viewpoint 283), where the flowbased blending performs slightly worse than the regular blending, even though the viewpoint



Figure 4.37.: Bottom face of synthesized point 145: The flow-based blending introduces a distortion on the blue table which extends to the radiator (green). Otherwise the results are very similar. For more details see Figure A.15 (page 108).

is located near the center of the grid cell. Part of the cause for this is a severe displacement artefact in the flow-based blending result, which decreases the accuracy. Other than this, the images are extremely similar. Figure A.14 on page 107 shows the resulting images at this viewpoint.

Finally, the most unexpected case: directly adjacent to a captured viewpoint, the flowbased blending performs worse than the regular blending according to both the L1 and SSIM error metrics. Figure 4.37 shows the bottom face of viewpoint 145, which is near the top left corner of the room, above the blue table. The results of the regular and flow-based blending are very similar, except some distinct artefacts in the flow-based blending result, where the blue table shows a distortion extending in different directions (marked in green). The rest of the results of this viewpoint, shown in Figure 4.37 on page 108, are very similar. Viewpoint 504, which is also directly adjacent to a captured viewpoint near the bottom right of the room, also has barely visible differences between the two results, which can be seen in Figure A.16 on page 109. In this case, the black line artefacts may again be part of the reason why the flow-based blending result has a higher error value.

Scenario Synopsis In summary, in this scenario, the results of the flow-based blending generally yield lower error values than the regular blending results in areas close to objects and walls, as well as in areas farther away from captured viewpoints. On the other hand, the regular blending generally performs better than the flow-based blending in close proximity to captured viewpoints. This is more pronounced towards the center of the scene, where the regular blending generally performs better due to higher distances to detailed objects. However, since the results of both techniques are visually very similar near captured viewpoints, it is possible that the worse performance of the flow-based blending is in part due to the external library bug, which introduces black lines and a slight pixel offset in only the flow-based blending results. The other reason for the worse performance of the flow-based blending algorithm near captured viewpoints is likely to be the introduction of discontinuities due to the choice of input viewpoints for the 1-DoF interpolation.

4.3.4. Discussion

The evaluation of the three scenarios using virtual data gives a first impression of the general performance of the flow-based blending compared to the regular blending under different circumstances, as well as indicating some of the basic problems and challenges of the flow-based approach.

In many of the tested cases the flow-based blending produces lower error values than the regular blending. However, the evaluation also uncovers some factors that decrease the accuracy of the flow-based blending results, originating from the implementation details as well as the underlying approach. The most important of these factors are:

- failure of the optical flow algorithm
- bugs in one of the external libraries
- deviation-angle-based choice of input viewpoints with abrupt change
- ray approximation

In general, there are certain objects in the square and oblong rooms for which the Blender optical flow yields better results than for others. A notable example is the rug, which is synthesized with clear edges without warping or blurring effects in all of the examined images (there are some discontinuities, but these are not due to the 1-DoF interpolation). The coffee table is an example for the optical flow being partially accurate, since it is often synthesized in an accurate position, but with blurred details. For the bookshelf, on the other hand, the Blender optical flow almost always yields inaccurate results, which results in warped, blurry, and distorted areas. It is clear that the accuracy of the flow-based blending results is directly dependent on the accuracy of the optical flow used in the 1-DoF interpolation, so it is very likely that better results can be achieved with a more accurate optical flow algorithm.

Another external factor that may cause elevated error values for the flow-based blending is a reprojection problem in the external library Skylibs [Hol20]. This bug leads to slight pixel offsets and thin black lines in the flow-based blending results, exclusively, as the regular blending does not use the problematic operation. As a result, it may have a noticeable impact on the $\Delta L1$ and $\Delta SSIM$ error values in cases where the results are very similar. However, this error is very difficult to quantify, since the flow-based blending result contains strips of a number of 1-DoF interpolated images, which display the problem to varying degrees. As a result, it can only be assumed that this bug may have a noticeable impact on the accuracy of the flow-based blending results.

The accuracy of the optical flow and the effect of the bug in the external library are both implementation-related problems, as they are not part of the approach, and may be improved by using different algorithms or libraries. However, there are also some problems that are intrinsic to the approach, and thus need to be discussed in more detail.

One of the most common artefacts in the flow-based blending results are severe discontinuities and jumps. This type of artefact is caused by the choice of input viewpoints for the 1-DoF interpolation. Figure 4.38 breaks down the cause of the problem step by step: Figure 4.38a shows an arbitrary synthesized viewpoint in the oblong room that displays this problem. Here, the abrupt discontinuities are clearly visible, for example on the rug in the bottom and right faces. In the synthesis process for each pixel of this image, two viewpoints A and B are chosen that are on either side of the ray corresponding to the pixel



(a) A viewpoint in the oblong room with visible discontinuities



(c) The panels of the image that have been assigned to a set of input viewpoints $\mathbf{A}, \mathbf{B} \in [13, 14, 19, 20]$



(b) The rays in the scene at which the choice of viewpoints switches (approximated)



(d) The panels applied to the image

Figure 4.38.: The input viewpoint choice problem in the oblong room

(explained in detail in Section 3.1.3). If more than one viewpoint is found on either side of the ray, the points with the smallest deviation angles are chosen. The interpolation distance between these points A and B is then calculated and the 1-DoF interpolation is performed. Finally the interpolated point is reprojected to the position of the synthesized viewpoint. This succession of operations is performed for *each ray* (i.e., each pixel) of the synthesized image. As a result, there are areas in the synthesized image, where, from one pixel to the next, a different set of input viewpoints is chosen. Figure 4.38b shows the synthesized point in the scene (the oblong room), along with the (approximated) rays where the choice of input viewpoints changes. The surrounding captured viewpoints are viewpoints 13, 14, 19 and 20. This process leads to image areas ("panels") originating from a 1-DoF interpolation between different sets of input viewpoints (Figure 4.38c). When applying these panels to the synthesized image (Figure 4.38d), it becomes clear that these are the source of the abrupt discontinuities.

The switch between viewpoint sets within the image does not always seem to be a problem. For example, when comparing a very similar viewpoint from the square room with the example from the oblong room, (Figure 4.39), some discontinuities are hardly visible, for example at the coffee table, or on the door. Other discontinuities are visible, but less noticeable, since the displacement is relatively small, for example on the rug, or on the TV cabinet. Since each panel is reprojected separately, it is possible that the severity of the discontinuity is dependent on the accuracy of the reprojection, which again is dependent on the difference between the scene geometry and the proxy geometry. This may explain why



(a) A similar viewpoint to Figure 4.38 in the square room



(c) The panels of the image that have been assigned to a set of input viewpoints $\mathbf{A}, \mathbf{B} \in [13, 14, 19, 20]$



(b) The panels visualized in the scene (approximation)



(d) The panels applied to the image

Figure 4.39.: The input viewpoint choice problem in the square room

the discontinuities are less severe in the square room than the oblong room, since the basic geometry of the square room is more similar to the proxy sphere than the basic geometry of the oblong room. However, since the scenario that evaluated the effect of the scene geometry focused mostly on objects within the scene instead of the basic scene geometry, no definitive assertion can be made at the moment.

The other possible source of inaccuracies, and a possible contributor to the displacements, is the ray approximation that is necessary for choosing the input viewpoints (detailed in Section 3.1.3). However, since the ray approximation is uniform for all of the flow-based images, it is difficult to judge how much of an impact it has on the results. Based on the analyzed images, it does not seem to create noticeable artefacts that can unambiguously be traced back to it.

4.4. Proof-of-Concept Evaluation Using a Real Scene

Following the extensive evaluation of the virtual scenes, this section presents the results of the 2-DoF synthesis tested on a real scene. The goal of this "proof-of-concept" evaluation is to determine to what extent the insights gained in the evaluation of the virtual scenes hold true for data captured in the real world.

As for the internal and external parameters, only a single scene is tested, using a grid of captured viewpoints with a single density. Within this grid, several viewpoints are synthesized at random positions, and the regular blending results are compared to the flow-based blending results.

4.4.1. Data Acquisition

The images were captured using a Ricoh Theta Z1 360° camera with a tripod in an approximately 3m by 2.5m room with a sloped roof and simple furnishings. An image taken near the center of the room is shown in Figure 4.40a. In order to have approximately uniform distances between the captured viewpoints, a 5x5 grid was mapped out on the floor. The spacing used for the grid is 40cm, as this is estimated to be a feasible distance for optical flow calculations. In order to capture ground truth data to compare the synthesized images with, the tripod was randomly placed within the boundaries of the grid, capturing 13 different viewpoints.

After acquiring the image data, the structure-from-motion library OpenSfM [Map20] was used to automatically determine the positions and rotations of all of the images. The positions of the ground truth viewpoints are then used as positions for the 2-DoF synthesis. Using the captured image data along with the estimated metadata, the synthesis can be performed. Instead of using a radius encompassing the complete area of the room, a slightly smaller radius is chosen so that the proxy geometry is closer to the actual scene geometry. Figure 4.40b shows the acquired scene, including the proxy geometry as a gray circle. The proxy geometry is centered around the points, which were captured slightly offset from the center of the scene.



(a) Latlong image from the center of the room



(b) The captured (blue) and synthesized (orange) viewpoints in the scene. The furnishings in the scene are an approximation.

Figure 4.40.: Overview of the real scene



Figure 4.41.: Scene analysis visualization the real scene.

4.4.2. Results

The same evaluation procedure used in the virtual scenes is used for the real scene: After synthesizing the images using the naïve algorithm, the regular blending algorithm and the flow-based blending algorithm, the L1 and SSIM error values are calculated using the ground truth data. Since there is only one setup to consider, the general tendencies of both the regular and flow-based blending results are discussed (e.g., why the error values are especially high for both blending types at a specific viewpoint), and then the results of the flow-based blending are compared to the results of the regular blending.

General Tendencies

Figure 4.41 shows the scene analysis visualization for the regular and flow-based blending. At a glance, the error values of the results of both methods are very similar. The error values of the viewpoints towards the left of the scene seem to be slightly lower than those on the right side of the scene, however, there is no clear pattern.

In order to get an impression of the general look and accuracy of a synthesized image in the real scene, one of the better rated points, viewpoint I near the top left corner is inspected. Figure 4.42 shows that both the regular blending, and the flow-based blending work fairly



Figure 4.42.: Viewpoint I (relatively low values for both regular and flow-based blending): Most of the scene is fairly accurate for both blending techniques. The largest positional inconsistencies are the tripod (magenta) and outside of the windows (cyan). The exernal library bug also causes very visible artefacts in the flowbased result (green).



Figure 4.43.: Right face of viewpoint'D (high values for both regular and flow-based blending): The high error values are due to the proximity to the cabinet, which is not reprojected correctly in the regular blending, and for which the optical flow algorithms also seems to have failed.

well in this case: Most of the objects are positioned accurately, the largest error being on the tripod in the bottom face (marked in magenta), which is not really of interest since it is not actually part of the scene, and on the windows (marked in cyan). The windows have a comparatively high error, not necessarily because they are synthesized incorrectly, but mostly because the lighting is different between the captured viewpoints and the ground truth viewpoints⁶. The black lines from the external library bug (marked in green) are unfortunately fairly disrupting visually, since most of the background is white, which makes them stand out (which will also contribute to a higher L1 value).

A closer look at Figure 4.41 shows that viewpoint D has particularly high error values for both metrics. The high error values for both methods for this viewpoint are due to the proximity of the cabinets to viewpoint D, shown in Figure 4.43. Unsurprisingly, the regular blending does not correctly reproject the cabinets, since they are not represented by the proxy geometry. However, the flow-based blending also fails, presumably because the displacement between the input viewpoints is too large for the optical flow algorithm to handle. The rest of the faces, shown in Figure A.17 on page 110, are very similar.

The rest of the viewpoints have similar values as viewpoint I, meaning they presumably yield fairly accurate results for both blending methods.

Comparing Regular Blending to Flow-based Blending Results

The boxplot in Figure 4.44 shows the distribution of the error values of the results of the naïve algorithm, the regular blending, and the flow-based blending. At a glance, it is clear that the regular and flow-based blending once again perform better than the naïve blending algorithm. However, the error values of the regular and flow-based blending are extremely

⁶The changes in illumination are due to the timing of the captures: The ground truth images were captured after the input viewpoints, when there was already less daylight. As a result, the synthesized viewpoints (which use the more illuminated captured viewpoints as input) are compared to the "ground truth" viewpoints that have less illumination from outside the window.



Figure 4.44.: Distribution of the error values of the results from the real scene

close, and the distribution is inconclusive.

The scene analysis visualization in Figure 4.45 shows the $\Delta L1$ and $\Delta SSIM$ of the flowbased blending compared to the regular blending. For most of the viewpoints, the flow-based blending performs slightly better than the regular blending for both metrics. However, all of the values are very close together, and the difference between the highest and lowest $\Delta L1$ and $\Delta SSIM$ is generally very small. In this case, the error values alone are not sufficient to understand the differences between the regular versus the flow-based blending.

Viewpoint G, which is near the middle of the scene, shows distinctly higher L1 error values for the flow-based blending. In this viewpoint, most of the details are slightly more accurate in the flow-based blending result. However, like in the virtual scenes, the flow-based blending also introduces some artefacts. The probable reason for the high L1 error for the flow-based blending result is the extreme ghosting on the top face, shown in Figure 4.46, where the 1-DoF interpolation was not able to correctly calculate optical flow of the ceiling lamp. The large RGB difference of the pixels of the ceiling lamp in the flow-based blending result is most likely also the reason why the $\Delta L1$ error value is significantly higher than the $\Delta SSIM$ value for viewpoint G. Figure A.18 on page 111 shows more details of this viewpoint.

Viewpoint A, near the bottom left corner, has a relatively high $\Delta L1$ and $\Delta SSIM$ (i.e., decrease in accuracy for flow-based blending). This result also clearly demonstrates two of the problems of the flow-based blending: There is some distortion due to failed optical flow, and there are clearly visible discontinuities. The result is shown in Figure A.19 on page 112.

Viewpoint K, near the right side of the room, is an example where the flow-based blending performs better than the regular blending. The left face of the regular blending result, depicted in Figure 4.47, shows a distinct inaccuracy in the shape of the lamp, which is accurate in the flow-based blending result. Also, the area around the lamp, including the small table and the edge between the wall and the floor, is more accurate in the flow-based blending result. The rest of the faces, shown in Figure A.20 on page 113 are visually very similar.

Judging by the inspected results, it is likely that the remaining results show similar patterns: The flow-based blending results perform better than the regular blending result in some areas, but failed optical flow, discontinuity artefacts, and possibly artefacts due to the external library bug prevent the flow-based blending results from being unambiguosly more accurate.



Figure 4.45.: $\Delta L1$ and $\Delta SSIM$, "improvement" of flow-based blending results over regular blending results for the real scene.



Figure 4.46.: Viewpoint G (L1 much higher for flow-based blending, SSIM only slightly higher): The failed optical flow on the ceiling lamp in the top face is likely the reason for the significantly higher L1 error value. For more details, see Figure A.18 on page 111.



Figure 4.47.: Viewpoint K: The shape of the lamp is more accurate in the flow-based blending result, and the whole area around the lamp (the small table and the edge between the walls and floor) is also in a more accurate position. For more details see Figure A.20 (page 113).

4.4.3. Discussion

In summary, the proof-of-concept evaluation shows that the insights gained in the evaluation of virtual scenes hold true in the real scene: In a number of cases, the flow-based blending performs better than the regular blending, according to the L1 and SSIM metrics. Visually, the flow-based blending manages to improve some of the artefacts caused by using the proxy geometry; however, it also introduces artefacts originating from the abrupt change in input viewpoints for 1-DoF interpolation, which are visually irritating. Also, in the places where the optical flow algorithm fails, the results are blurred or warped, which is visually more noticeable than the regular blending result, where the objects are left undistorted but possibly viewed from an inaccurate perspective. Nonetheless, the evaluation in the real scene shows that 1-DoF interpolation can be used in order to improve the accuracy of basic pixel-based synthesis.

4.5. Limitations of the Evaluation

An evaluation is only ever as significant as the parameter space it covers and the metrics it uses. In this case, the evaluation uses a relatively small parameter space, and tests the results using predominantly mathematical, pixel-based error metrics. This limits the significance of the evaluation in the following ways:

Firstly, only a limited number of external parameters are tested, for example leaving out more extreme room shapes that deviate strongly from the basic rectangular shape. It is possible that, given a strong deviation from the proxy geometry, the artefacts in the flowbased blending caused by the abrupt change in input viewpoints would increase to a degree where the regular blending would be preferable. Also, only indoor scenes are considered. It is possible that the behavior of the algorithms is completely different for outdoor scenes with much larger distances between the viewpoint and the scene geometry. Furthermore, the parameters that are tested are not tested exhaustively, so it is possible that some interactions between parameters are overlooked.

Secondly, the metrics that are used (i.e., the L1 error and the SSIM error), can show an improvement between different results, but it is difficult to quantify this improvement. For example, it is not possible to explicitly compare the error values of different scenes (unless they contain very similar colors and patterns), since the L1 error metric is very dependent on pixel color values, and it is difficult to differentiate the exact cause-and-effect of the SSIM error metric. Futhermore, the L1 and SSIM error metrics give no indication on believability or visual preference, since they cannot measure the severity of artefacts for human perception. This means that it is possible that users may prefer the regular blending results over flow-based blending results, due to the smoother transitions of the regular blending between different areas. Although user acceptability is not a criterium for this evaluation, it is crucial for the intended area of appliation, namely Virtual Reality. Another factor that plays into the visual acceptability is temporal consistency, i.e., whether the parallax movement of objects in the scene is believable when navigating through the scene using synthesized views. This is also not tested in the evaluation.

Lastly, due to the bug in the external library, the results of the flow-based blending have an unquantifiable disadvantage. It is possible that an implementation without the bug would perform significantly better, but it is also possible that the bug has no significant impact.

5. Conclusion and Future Work

Synthesizing planar and 360° images by interpolating with optical flow has been used in a number of different approaches in the past. The synthesis approach presented in this thesis, however, is a combination of flow-based interpolation with pixel-based 2-DoF synthesis, which is unique in the related work, summarized in Table 5.1: The method columns (1-3) of Table 5.1 show that most approaches either provide 2-DoF without using extracted image features, or extract optical flow but only provide 1-DoF. The idea behind the pixel-based 2-DoF synthesis with flow-based blending developed in this thesis is to mitigate artefacts caused by inaccurate scene geometry by generating viewpoints with more accurate perspectives.

The evaluation of this approach differs from the evaluations of the majority of other approaches, summarized in the evaluation columns (4-7) of Table 5.1: Other approaches generally test their methods on a minimal set of images, only sometimes declaring the parameters that were used, and in almost every case using visual examination exclusively to evaluate their results. In this thesis, the evaluation defines a clear parameter space and evaluates the results using mathematical error metrics as well as visual evaluation. The comparison of this flow-based method to a basic pixel-based method uncovers the strengths and limitations of the flow-based blending method; however, this approach is not compared to any of the other methods shown in Table 5.1, which is why the checkmark in the last column of the table is in parentheses.

The parameter evaluation on virtual scenes in this thesis tests the effect of scene geometry, captured viewpoint density and the relative position of synthesized viewpoints to captured viewpoints on the accuracy of the results. In general, the flow-based blending algorithm presented in this thesis improves the results of the basic method especially where the actual scene geometry differs more significantly from the proxy geometry (e.g., near walls and objects) and if the synthesized viewpoint is not in the close vicinity of a captured viewpoint. Based on the insights gained in the parameter evaluation on virtual scenes, a real scene is tested as well, which shows that the synthesis with flow-based blending also improves the majority of results of the basic algorithm when using real data.

Future Work

The evaluation provides insights into the strengths and limitations of this approach, which can be used in the future in order to improve the approach, implementation and evaluation of the pixel-based 2-DoF synthesis using flow-based blending.

The most obvious limitation of the approach is the reliance on accurate optical flow. The optical flow algorithms used in this thesis do not always manage to provide accurate optical flow, which has a noticeable impact on the results. It would be advantageous to explore different optical flow algorithms, especially ones that focus on capturing large displacements. For example, there are many optical flow algorithms based on Deep Learning techniques [SET20] that could yield more accurate optical flow than conventional methods. Furthermore, it could be possible to undistort the extended cube map before calculating optical flow

5. Conclusion and Future Work

	method			evaluation			
	input type	DoF	extracted features	defined parameter space	visual eval.	error metrics	comparison to other approaches
[Kaw17]	360° images	2	none	×	1	×	×
[SLDL09]	360° images	2	none/ dense geo	×	1	×	×
[HDR ⁺ 17]	360° images	2	none	×	×	×	×
[RPZSH13]	planar images	1	dense flow	×	1	×	\checkmark
[KL10]	360° images	1	dense flow	×	1	1	×
[HCCJ17]	360° video	3*	dense geo	×	1	×	✓
[ZWF ⁺ 13]	360° video	1	sparse feature	×	1	1	✓
Pixel-based synthesis with flow-based blending (this thesis)	360° images	2	dense flow	1	1	1	(✓)

*on a constrained path

Table 5.1.: Comparison of this thesis to the related work presented in Section 2.2

(e.g., by using a method like the one presented in [SLL19]), which could also improve the accuracy of the optical flow result on the extended cube maps.

The other, visibly most detrimental limitation of the presented approach is the effect of the abrupt change in the selection of input viewpoints for 1-DoF interpolation, which results in visual discontinuities. In order to reduce these discontinuities, one possible approach would be to use proxy geometry that is closer to the scene geometry, that could for example be approximated using a structure-from-motion algorithm to calculate sparse scene geometry. By using a more accurate reprojection, the discontinuities would most likely be lessened. An alternative would be to change the selection of input viewpoints for the 1-DoF interpolation, or to introduce some kind of constraint (e.g., a color constraint) in order to blend and soften the abrupt edges.

As for more implementation-related improvements, most synthesis techniques are used in real-time, which the proof-of-concept implementation presented in this thesis does not support. However, the implementation offers many opportunities for parallelization and the offloading of operations to the GPU, and more could be found by profiling the implementation. Leveraging these opportunities would be very advantageous, as this could enable real-time navigation, opening up more possibilities for testing and evaluation based on visual perception.

By applying these improvements to the approach and implementation, an improved evaluation could be carried out, specifically in terms of the parameter space and the error metrics. Since the evaluation of different scenes mostly focuses on elements within the scene instead of the general scene shape, it would be interesting to explore the effect of the general scene shape. Furthermore, the impact of the ray approximation could be evaluated by comparing the accuracy of different areas of the result images. Finally, subjective perception is a key factor for Virtual Reality applications, since it is important for users to accept and believe the synthesized images. Performing a user study would enable an evaluation that is more specific to the needs of a Virtual Reality application.

The insights gained from the development and evaluation of the pixel-based 2-DoF synthesis with flow-based blending can be used to improve various geometry-based algorithms, and potentially even be combined with cutting-edge Deep Learning technologies. This could help enable casually captured environments to be explored interactively, which could enhance a broad range of Virtual Reality applications, allowing users to immersively experience remote locations, historical landmarks, and foreign cityscapes around the world.

A. Synthesized Images

A. Synthesized Images



(a) Image A at viewpoint **A**



(c) Optical flow vectors $F_{A \to B}$



(e) The shifted image I_A (the black edges are due to pixels past the image with no value being shifted into the image)



(b) Image B at viewpoint ${\bf B}$



(d) Optical flow vectors $F_{B\to A}$



(f) The shifted image I_B



(g) The final interpolated image S at δ = 0.5 between images A and B

Figure A.1.: An example of 1-DoF flow-based blending at interpolation distance $\delta=0.5$ between two planar images

square room



Figure A.2.: Flow-based blending result of viewpoint O in the square and oblong rooms: The bookshelf has a strong impact on the difference in error values (green) and the details of the bookshelf are warped due to inaccurate optical flow (magenta).



Figure A.3.: Synthesized point A in the oblong room (best improvement): The flow-based blending drastically improves ghosting artefacts on the couch (magenta) and the accuracy of the rug (cyan), but also introduces new artefacts (green).


Figure A.4.: Synthesized point L in the oblong room (worst improvement): The flow-based blending result introduces some severe discontinuity artefacts on the rug (magenta) and on the coffee table (cyan), although the coffee table is positioned more accurately in the flow-based blending result (green)



Figure A.5.: Synthesized point N in the square room (best improvement for L1, good for SSIM): The flow-based blending removes the ghosting artefacts on the rug (magenta) and improves the accuracy on the coffee table (cyan), and the lower part of the bookshelf (green). The rest of the scene is very similar for both results.



Figure A.6.: Synthesized point L in the square room (worst "improvement": slight increase of error for both metrics): The ghosting artefact on the rug in the regular blending result is replaced by a discontinuity artefact in the flow-based blending result (magenta), which also introduces a new artefact, namely the warped top edge of the coffee table (green). Otherwise the scenes are very similar.



Figure A.7.: The regular blending results for point T (one of the worse results) in the square room with different viewpoint densities: The 2x2 image shows the bookshelf from the wrong perspective (green), and the walls are noticeably warped (cyan), which is improved in the 6x6 and 12x12 images. The bookshelf is more accurate in the 12x12 image than the 6x6 image (magenta), but still shows some inaccuracies.



Figure A.8.: The regular blending results for point G (one of the better results) in the square room with different viewpoint densities: Both the accuracy and the ghosting effects are visibly reduced, the higher the density of the captured viewpoints is. This is especially clear for the coffee table (green).



Figure A.9.: Synthesized point T in the 2x2 setup (best improvement for L1, good for SSIM): The flow-based blending synthesizes a blurry approximation of the bookshelf (green), but also distorts and blurs the rest of the image (magenta), due to inaccurate optical flow from captured viewpoints with a too-large distance.



Figure A.10.: Synthesized point K in the 2x2 setup (worst "improvement": slight increase of error): Although the regular blending result shows many doubling artefacts and incorrect positioning problems, the results of the flow-based blending are visually much worse due to inaccurate optical flow.



Figure A.11.: Synthesized point Y in the 12x12 setup (best improvement for L1 and SSIM): The flow-based blending result synthesizes the bookshelf slightly more accurately (magenta), and also does not display an artefact present in the regular blending result (green), which appears due to the use of an input viewpoint that had small deviation angles in that area, but seems to have captured a part of the bookshelf with the respective rays. Other than that, the results are very similar.



Figure A.12.: Synthesized point H (worst "improvement": slight increase of error): The flowbased blending result synthesizes the coffee table and white pillow with cleaner edges (magenta), however, due to a bug in an external library, the flow-based blending result contains some black lines (green) that possibly skew the error values in favor of the regular blending.



Figure A.13.: Synthesized point 7: The accuracy of the pictures on the wall is better in the flow-based blending result (magenta), and the shapes and position of the rug and the coffee table are also more accurate (green). However, the black line artefacts (cyan) are also fairly severe.



Figure A.14.: Synthesized point 283: Apart from a severe displacement artefact in the regular blending image, which also decreases the accuracy on the coffee table, the results are very similar.



Figure A.15.: Synthesized point 145: The flow-based blending introduces a slight displacement on the coffee table (magenta) and a distortion on the blue table (green). Otherwise the results are very similar.



Figure A.16.: Synthesized point 504: The position of the coffee table in the flow-based blending result is less accurate than in the regular result (green). Otherwise the results are almost identical, except for the black lines caused by the external library bug (magenta).



Figure A.17.: Viewpoint D (high values for both regular and flow-based blending): The high error values are due to the proximity to the cabinet, which is not reprojected correctly in the regular blending, and for which the optical flow algorithms also seems to have failed (magenta).



Figure A.18.: Viewpoint G (L1 much higher for flow-based blending, SSIM only slightly higher): Most elements of the scene are more accurate in the flow-based result (magenta), however, it does introduce some artefacts, including on the door and wall (green) and on the ceiling lamp, where the optical flow is inaccurate (cyan).



Figure A.19.: Viewpoint A (error values higher for flow-based blending): The flow-based blending result shows some ghosting artefacts due to failed optical flow (magenta), and discontinuities (green), but also has a more accurate positioning of the cabinets (cyan).



Figure A.20.: Viewpoint K (flow-based blending produces better results than the regular blending): The shape of the lamp is more accurate in the flow-based blending result (green), and the whole area around the lamp (the small table and the edge between the walls and floor is also in a more accurate position.

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